

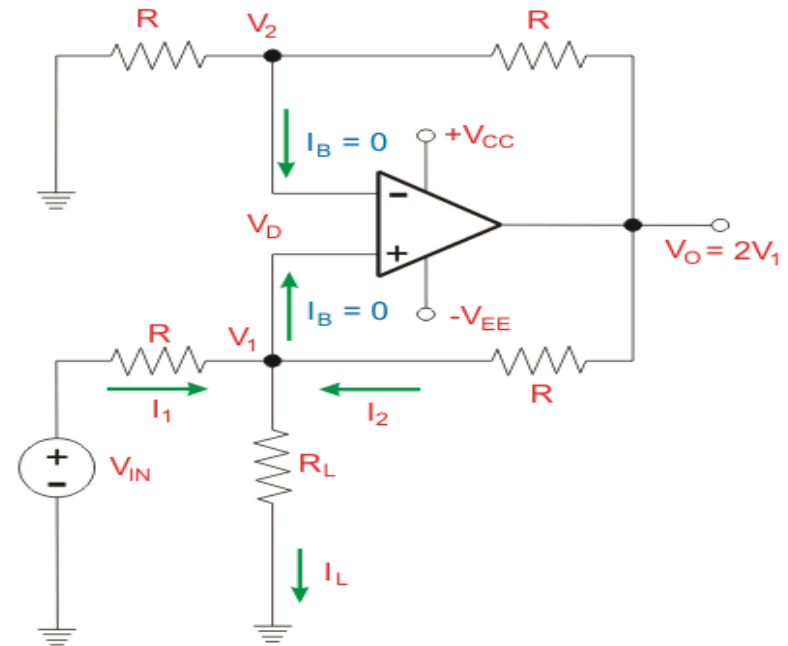
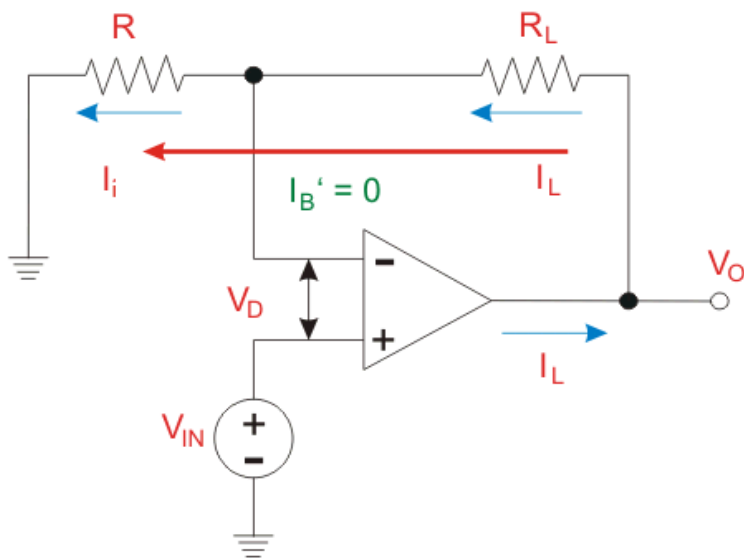
# MODULE 3-ANALOG INTEGRATED CIRCUITS

CREDITS-4

COURSE CODE: EC 204

# VOLTAGE TO CURRENT CONVERTER

- ▶ Called Transconductance amplifier
- ▶ By application of voltage essential current is sustained throughout the circuit
- ▶ Convert voltage to a proportional o/p current.
- ▶ (a) With floating load
- ▶ (b) With grounded load



$R_L$  is floating (not linked to the ground)  $V_{in} = I_L \cdot R$  ( $I_B = 0$ ) i.e.  $I_L = V_{in} / R$  ( $V_i \rightarrow I_L$ )

Same current flows thru signal source and load. So this load current is provided back.

$I_i = I_L$

# Continued....

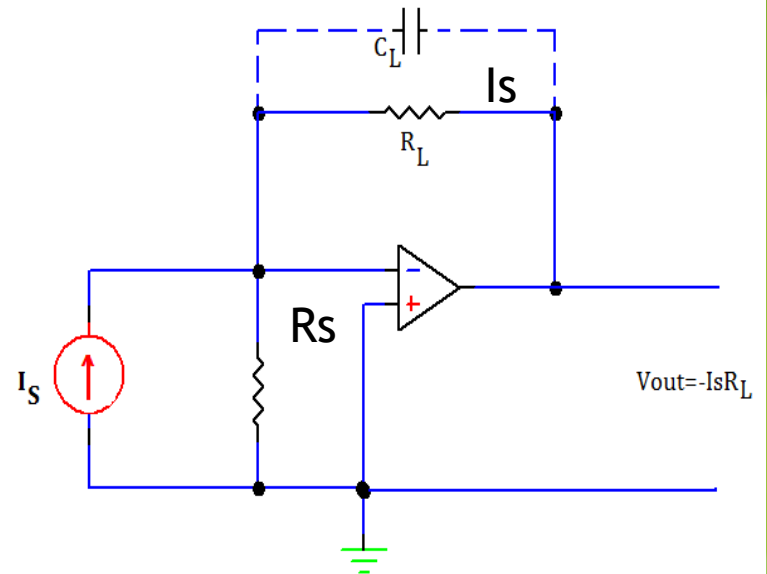
- ▶ one end of the load is always grounded.
- ▶ connection between the input voltage and load current.
- ▶ Opamp is in non inverting mode and  $gain=1+R/R=2$
- ▶  $I_1+i_2=i_L$  or  $(V_{in}-V_1)/R+(V_0-V_1)/R=i_L$
- ▶ O/p voltage ,  $V_0=2V_1$ -----2
- ▶  $(V_{in}-2V_1+V_0)/2=i_L * R$ -----1
- ▶ Substitute 2 in 1
- ▶ As input impedance of non inverting amplifier is very high ,it draws very little current from the source.
- ▶ the current  $I_L$  is related to the voltage,  $V_{IN}$  and R.

$$I_L=V_{in}/R$$

- Applications:
- ▶ For low voltage dc and ac voltmeter
- ▶ Testing LED
- ▶ Zener diode tester
- ▶ Testing diodes

# CURRENT TO VOLTAGE CONVERTER

- ▶ Called Transresistance amplifier
- ▶ Conversion of light energy to o/p current. Current through these devices can be converted to voltage (such as in photo cell, photo diode, photo voltaic cell)
- ▶ Thus amount of light incident on the photo device can be measured
- ▶ Negative terminal is at virtual ground
- ▶ No current flows thru  $R_s$  and current  $I_s$  flows thru load resistor  $R_L$
- ▶ o/p voltage =  $-I_s \cdot R_L$
- ▶ Depending on the bias current, measurable lowest current is found out. ( $I_b = 3\text{nA}$ ) for 741 IC
- ▶  $C_L$  is to reduce high frequency noise and possibility of oscillations.



# Virtual Ground

- ▶ In opamps the term virtual ground means that the voltage at that particular node is almost equal to ground voltage (0V). It is not physically connected to ground. This concept is very useful in analysis of opamp circuits and it will make a lot of calculations very simple.
- ▶ concept is valid only when negative feedback is applied to opamp like in inverting amplifiers.

Virtual Ground	Real Ground
Virtual Ground is a concept that made for easy explantaion and calculation purposes.	Real Ground is a terminal which is physically connected to ground or earth which acts as the reference point for the entire circuit.
Voltage is <b>approximately</b> Zero	Voltage is Zero
Not able to sink infinite current	It is an infinite current sink
Not electrically connected to Ground	Electrically connected to Ground

# INTEGRATOR

▶  $V_{in} - 0/R1 + C_f dV_0/dt = 0$

▶  $dV_0/dt = (-1/R1C_f) V_i$

▶ Integrate both sides,

$$V_{out} = -\frac{1}{R1C1} \int_0^t V_{in} dt$$

▶ Thus o/p voltage is proportional to the time integral of the input. (inverting integrator.)

▶ R1 at the non inverting side, to minimize the effect of input bias current.

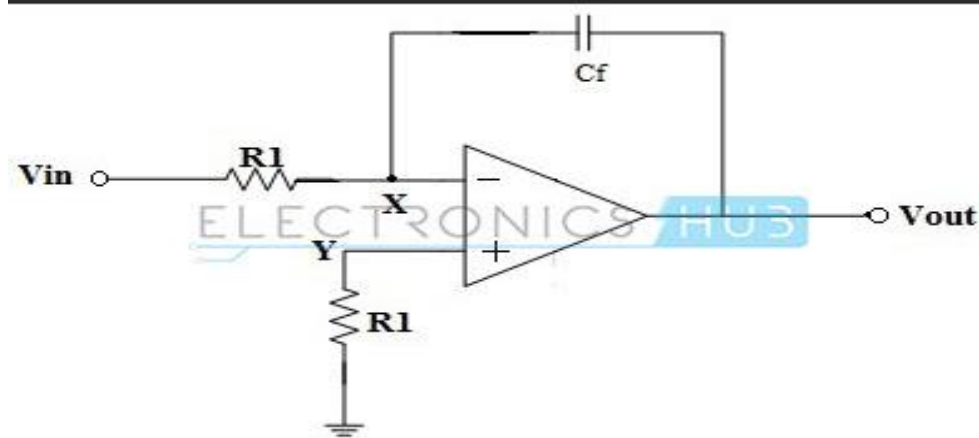
▶  $V_0(s) = -1/sR1C_f V_i(s)$

▶  $|A| = 1/wR1C_f$  ( $w = 2\pi f$ )

▶ Gain is inversely proportional to f

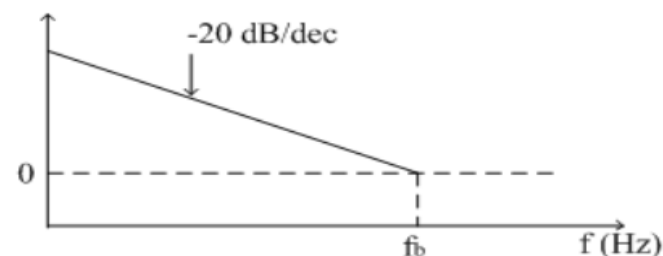
▶ At  $w=0, A = \infty$  / (At dc,  $C_f =$  open circuit so open loop gain becomes infinity)

▶ This problem of infinite gain will be solved by practical integrator circuit (lossy integrator)



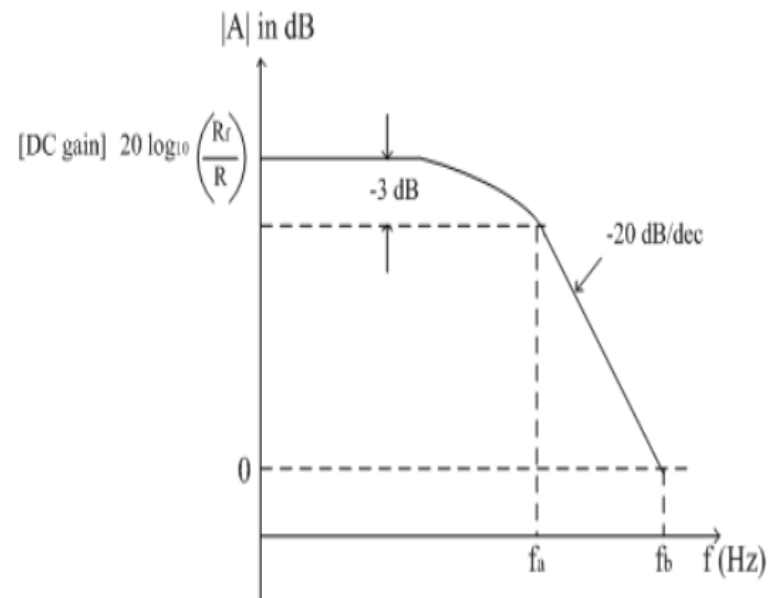
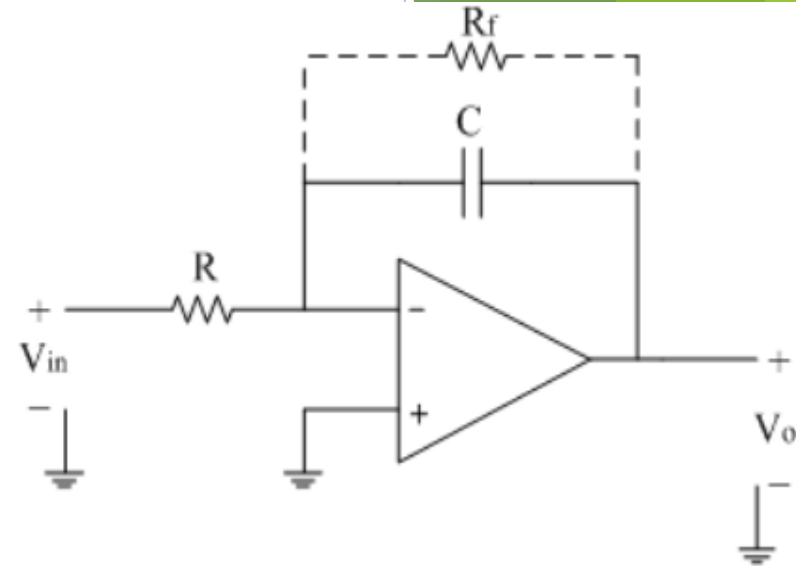
An Ideal Op-amp Integrator

|A| in dB



# PRACTICAL INTEGRATOR(LOSSY INTEGRATOR)

- ▶  $C_f$  is shunted by a resistor,  $R_f$
- ▶ Power dissipation is different for  $R_f || C$
- ▶  $V_{in}(s)/R + sC_f V_o(s) + V_o(s)/R_f = 0$
- ▶  $V_o(s) = (-1/(sRC_f + R/R_f)) V_i(s)$
- ▶ If  $R_f$  is large, lossy integrator will be equal to ideal integrator.
- ▶  $|A| = |V_o/V_i| = (R_f/R) / \sqrt{1 + (\omega RC_f)^2}$
- ▶ At low frequencies, gain is constant at  $R_f/R$ .
- ▶ Break frequency,  $f_a$  is the frequency at which gain is  $1/\sqrt{2}$
- ▶ By solving  $f_a = 1/(2\pi R_f C_f)$
- ▶ If  $f < f_a$ , circuit is like inverting amplifier



# DIFFERENTIATOR

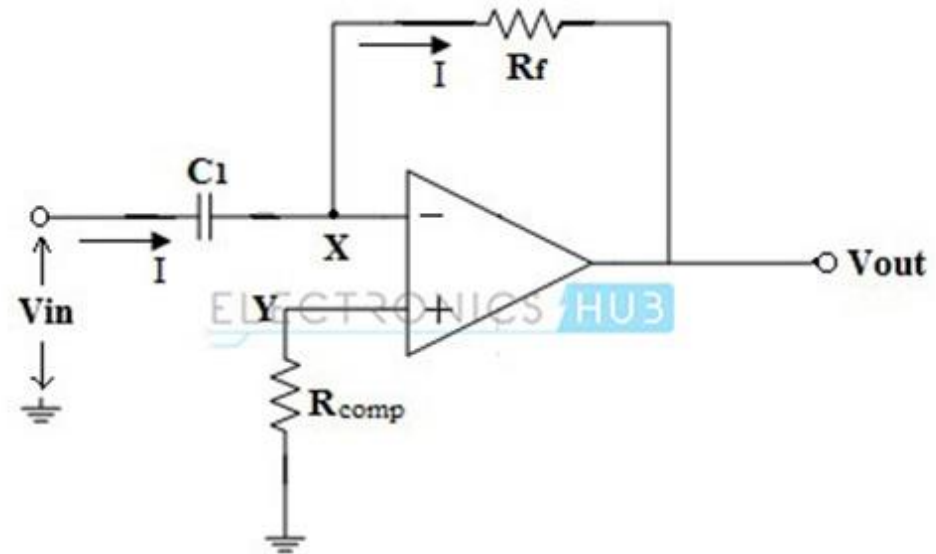
- ▶ Mathematical operation
- ▶ Output is the derivative of input
- ▶ Node X is at virtual ground
- ▶ Current through capacitor is

$$I = C_1 \frac{d}{dt}(V_{in}) + V_o/R_f = 0 \text{-----} 1$$

- ▶ No current into the opamp
- ▶  $V_o = -R_f C_1 \frac{dV_{in}}{dt}$
- ▶ Thus the name differentiator
- ▶ -ve sign indicates a 180 degree phase shift of the o/p waveform wrt i/p signal.
- ▶ Take Laplace Transform on both sides,

$$V_o(s) = -R_f C_1 s V_{in}(s)$$

- ▶  $|A| = |-j\omega R_f C_1| = \omega R_f C_1 = 2\pi f R_f C_1 = f/f_a$  where  $f_a = 1/2\pi R_f C_1$
- ▶ At  $f = f_a$ ,  $|A| = 1$  ie. 0dB
- ▶ Gain increases at a rate of +20dB/decade
- ▶ At high frequency, it becomes unstable and break into oscillation.
- ▶ Input impedance decreases with increase in frequency and circuit is sensitive to high frequency noise.





# PRACTICAL DIFFERENTIATOR

- ▶ Eliminates problem of instability and high frequency noise

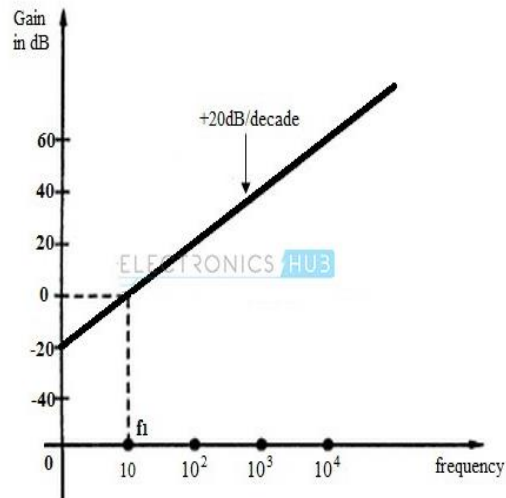


Fig: Frequency Response of Ideal Differentiator

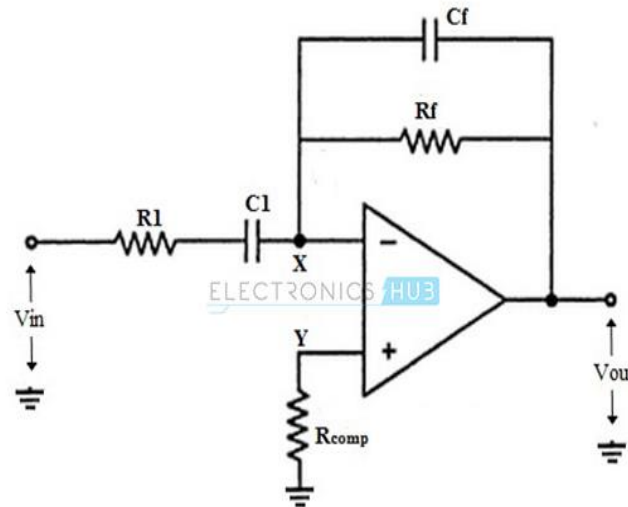


Fig: A Practical Op-amp Differentiator Circuit

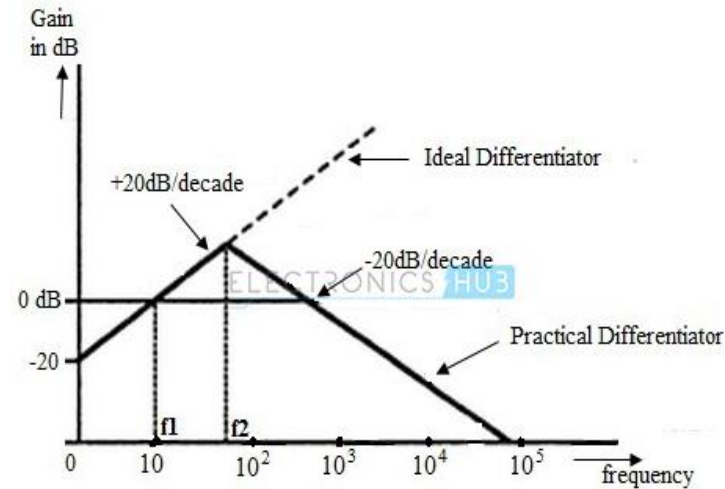


Fig: Frequency Response of Practical Differentiator

- ▶  $Z_f = R_f || C_f$      $Z_i = R_1 + C_1$
- ▶  $V_o(s)/V_i(s) = sR_fC_1 / (1 + sR_fC_f)(1 + sR_1C_1)$
- ▶ For  $R_fC_f = R_1C_1$ ,  $V_o(s)/V_i(s) = -sR_fC_1 / (1 + j(f/f_b))^2$

where  $f_b = 1/2\pi R_1C_1$

Gain increases at +20dB/decade for frequency  $f < f_b$  and decreases at -20dB/decade for  $f > f_b$

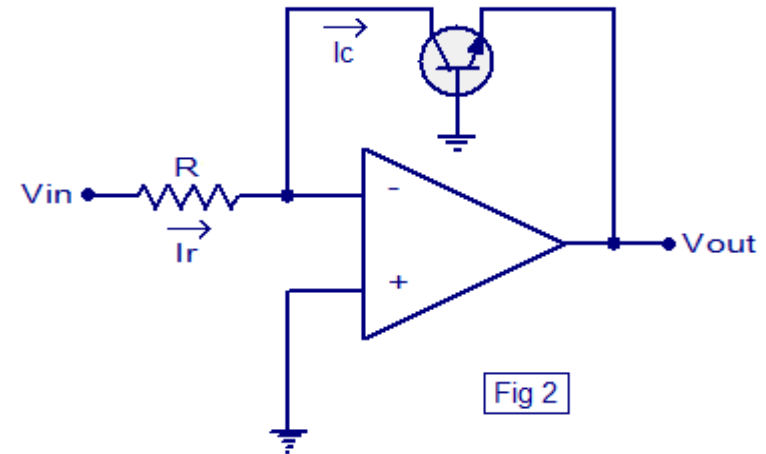
R<sub>comp</sub> –to reduce the i/p bias current

# LOG AND ANTILOG AMPLIFIERS

- ▶ Some functions like  $\ln x$ ,  $\log x$  and  $\sinh x$ -antilog amp
- ▶ Log amp-to compress the dynamic range of a signal
- ▶ LOG AMPLIFIER
- ▶ electronic circuit that produces a voltage at the output that is proportional to the logarithm of the voltage applied to the resistor connected to its inverting terminal
- ▶ A grounded base transistor is placed in the feedback path and collector is at virtual ground. So voltage current relationship is that of a diode

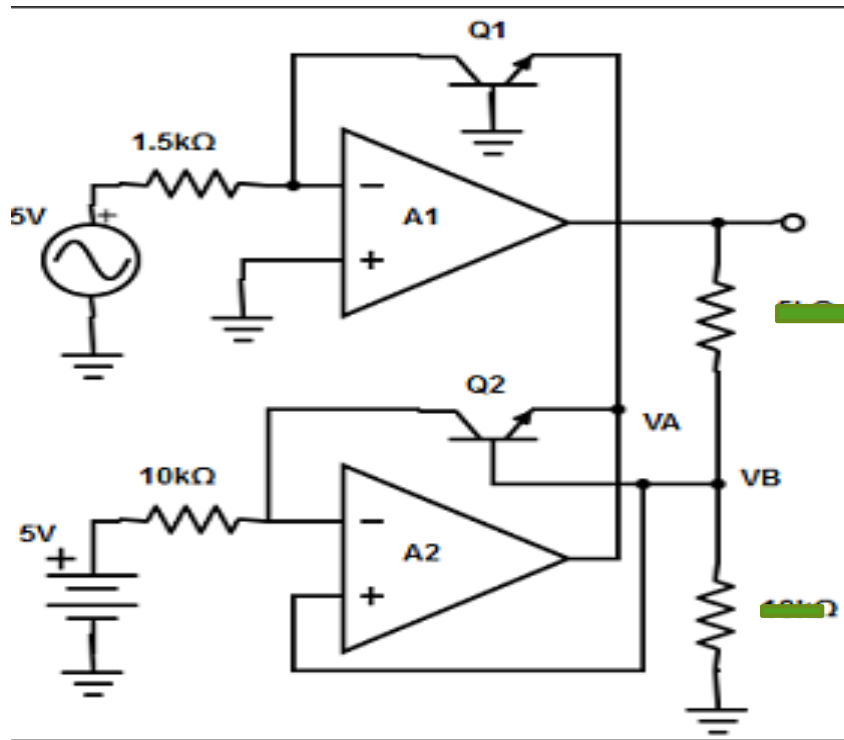
- ▶  $I_e = I_s(e^{(qV_e/kT)} - 1)$
- ▶  $I_c = I_e$  so  $I_c = I_s(e^{(qV_e/kT)} - 1)$
- ▶  $I_s$ -emitter saturation current.  $10^{-13}$
- ▶  $k$ -Boltzmann 's constant
- ▶  $T$ -absolute temperature in Kelvin
- ▶  $I_c/I_s = (e^{(qV_e/kT)} - 1)$
- ▶ As  $I_c \gg I_s$  so  $I_c/I_s = e^{(qV_e/kT)}$
- ▶ Take natural log on both sides,  $V_e = kT/q \ln(I_c/I_s)$
- ▶  $I_c = V_{in}/R$  and  $V_e = -V_o$  Thus  $V_o = -kT/q \ln((V_{in}/R)I_s) = -kT/q \ln(V_{in}/V_{ref})$

Where  $V_{ref} = R \cdot I_s$



# Limitation

- ▶ The emitter saturation current,  $I_s$  varies from transistor to transistor and with temperature. Thus a stable reference voltage  $V_{ref}$  cannot be obtained.



log amp using two opamps

$$V_o = (1 + R_2/R_{tc}) \frac{kT}{q} \ln(V_{in}/V_{ref})$$

## ANTILOG AMPLIFIER

- ▶ electronic circuit that produces a voltage at the output that is proportional to the anti-logarithm of the voltage that is applied to the diode connected to its inverting terminal.

# Continued....

- ▶ Input is fed into the temperature compensating voltage divider R2 and Rtc and to the base of Q2.

- ▶ Output is fed back to the inverting input of A1 thru R1

- ▶ Base emitter voltage of two transistors:-

$$V_{q1(b-e)} = (kT/q) \ln(V_o/R1 * I_s)$$

$$V_{q2(b-e)} = (kT/q) \ln(V_{ref}/R1 * I_s)$$

- ▶ Base of Q1 is grounded  $V_A = -V_{q1(b-e)}$

$$= -(kT/q) \ln(V_o/R1 * I_s)$$

- ▶ Base voltage of Q2,  $V_B = V_i (R_{tc}/(R2 + R_{tc}))$

- ▶ Emitter voltage of Q2,  $V_{q2(e)} = V_B + V_{q2(b-e)}$

$$= V_i (R_{tc}/(R2 + R_{tc})) + (kT/q) \ln(V_{ref}/R1 * I_s)$$

- ▶ This is  $V_A = V_{q2(e)}$

- ▶  $-(kT/q) \ln(V_o/R1 * I_s) = V_i (R_{tc}/(R2 + R_{tc})) + (kT/q) \ln(V_{ref}/R1 * I_s)$

- ▶  $V_i (R_{tc}/(R2 + R_{tc})) = -(kT/q) [\ln(V_o/(R1 * I_s)) - \ln(V_{ref}/(R1 * I_s))]$

- ▶  $-(q/kT) [R_{tc}/(R2 + R_{tc})] V_i = \ln(V_o/V_{ref})$

- ▶ Change natural log into log<sub>10</sub>

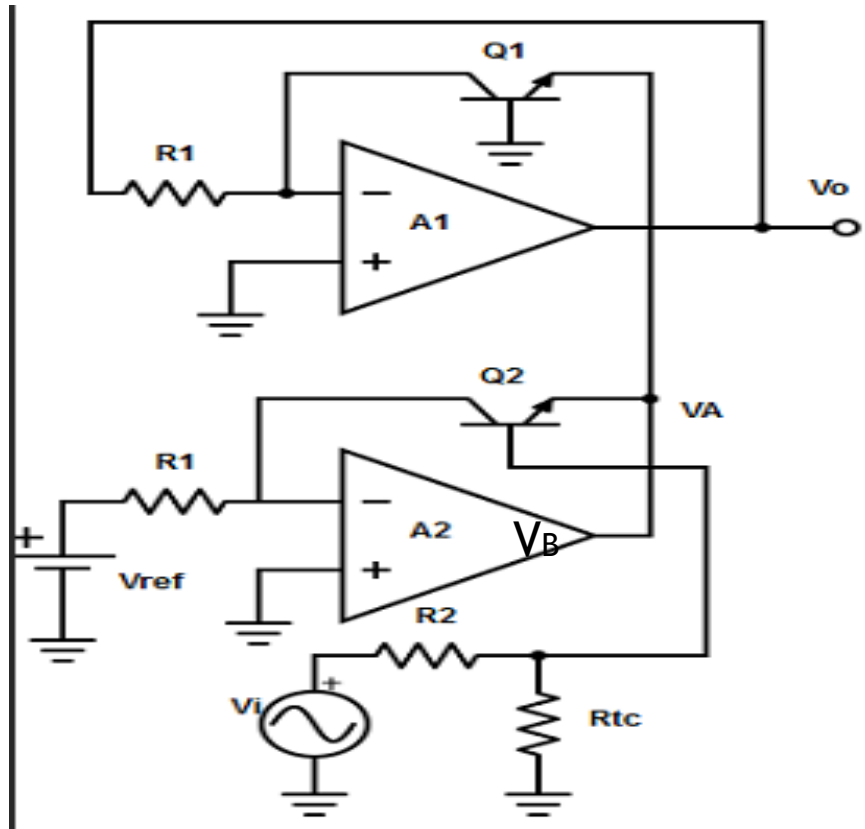
- ▶  $\log X = 0.4343 \ln X$

- ▶  $-0.4343 * (q/kT) [R_{tc}/(R2 + R_{tc})] V_i = 0.4343 * \ln(V_o/V_{ref})$

- ▶  $-K' V_i = \log (V_o/V_{ref})$

$$V_o = V_{ref} (10^{-K' V_i}) \quad \text{where } K' = 0.4343 (q/kT) [R_{tc}/(R2 + R_{tc})]$$

# Continued...



- ▶ An increase of input by one volt causes the o/p to decrease by a decade

# PRECISION RECTIFIER

- ▶ To rectify voltages below cut in voltage of the diode.
- ▶ Place a diode in the feedback loop of an opamp.
- ▶ Functions as a **Non inverting precision halfwave rectifier**.

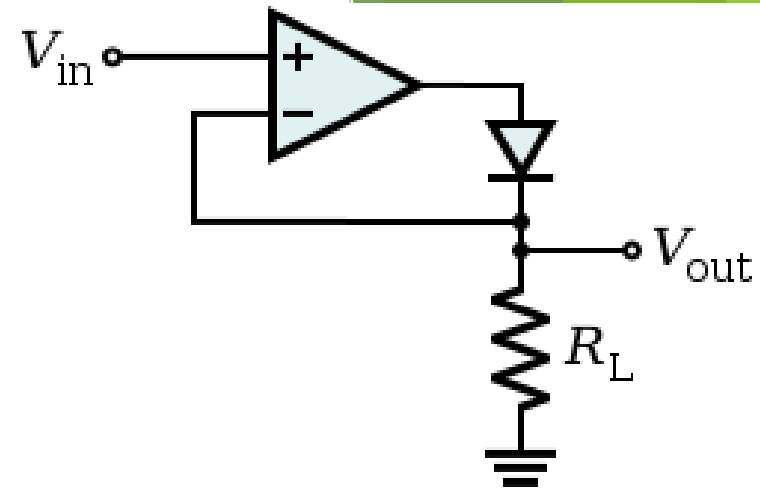
- ▶ When  $V_i$  is positive, opamp o/p is also positive.  $V_o = V_i$
- ▶ When  $V_i$  is negative, opamp o/p is also negative and Diode becomes reverse biased and  $V_o = 0$ .

Here cut in voltage becomes  $V_r/A_{ol} = 0.7/10^4 = 70\mu V$

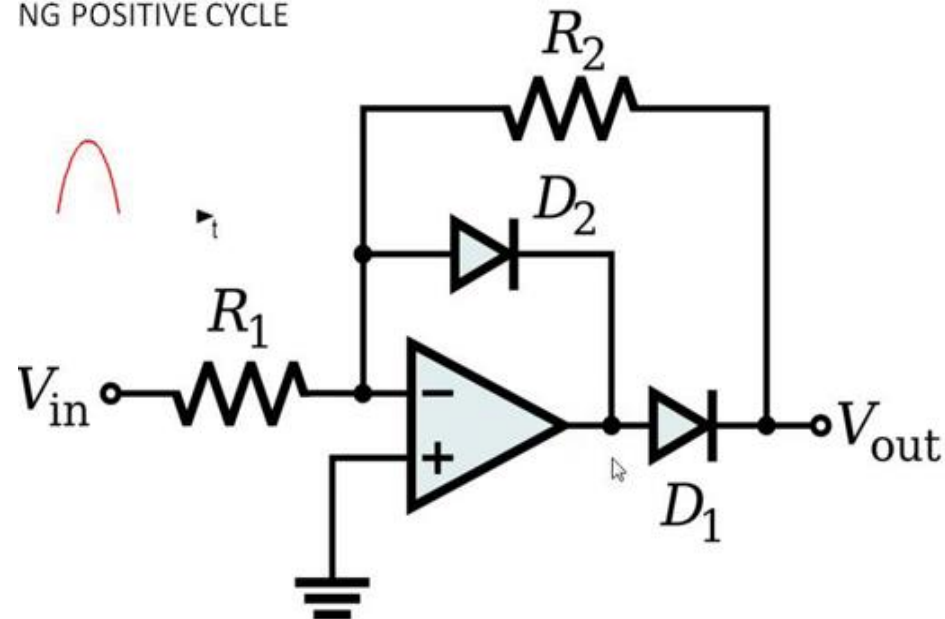
Conduction begins from a low voltage.

- ▶ **Inverting Precision Half wave rectifier:**

- ▶ When  $V_i > 0$ , opamp o/p becomes negative
- ▶  $D_2$  conducts and  $D_1$  reverse biased,  $V_o = 0$
- ▶ No current flows thru  $R_2$
- ▶ When  $V_i < 0$ , opamp o/p becomes positive
- ▶  $D_1$  conducts and  $D_2$  reverse biased
- ▶ So circuit acts like an inverting amplifier
- ▶ Gain =  $R_2/R_1$
- ▶ Advantages:
  - ▶ half wave rectifier
  - ▶ non saturating



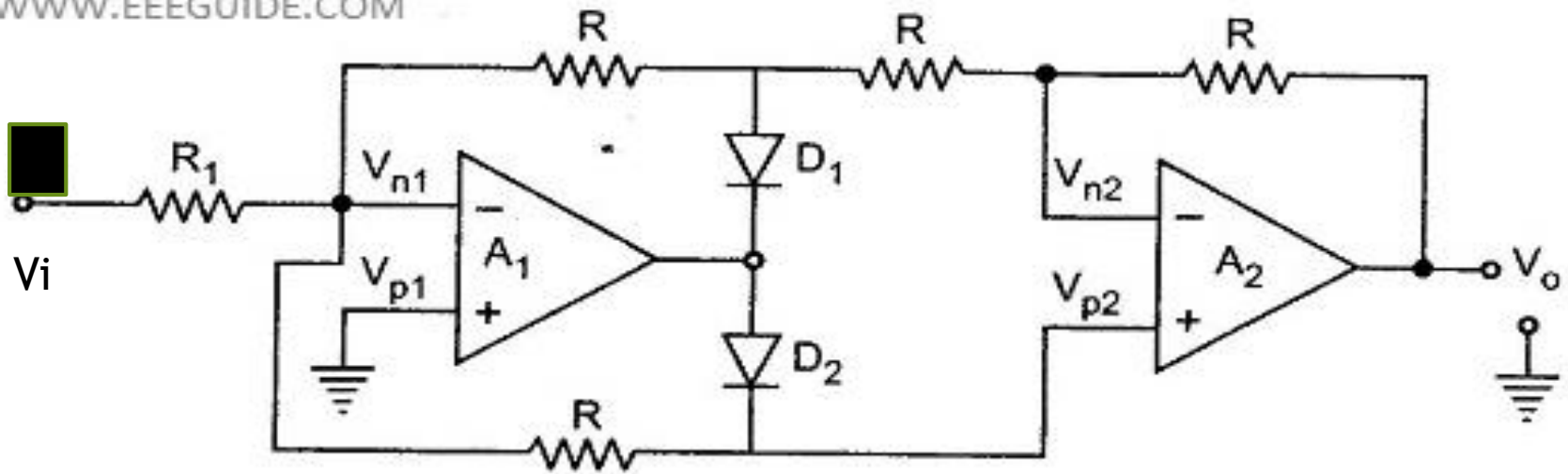
NG POSITIVE CYCLE



# FULL WAVE RECTIFIER

- ▶ Accepts ac signal either negative or positive, the o/p is obtained as Positive. It is called absolute value circuit.
- ▶ When  $V_i > 0$ ,  $A_1 = \text{negative}$
- ▶  $D_1$ -FB,  $D_2$ -RB and no current flows through resistance  $R$  connected between  $V_{n1}$  and  $V_{p2}$
- ▶  $A_1$  and  $A_2$  act as inverter giving positive o/p.  $V_o = V_i$

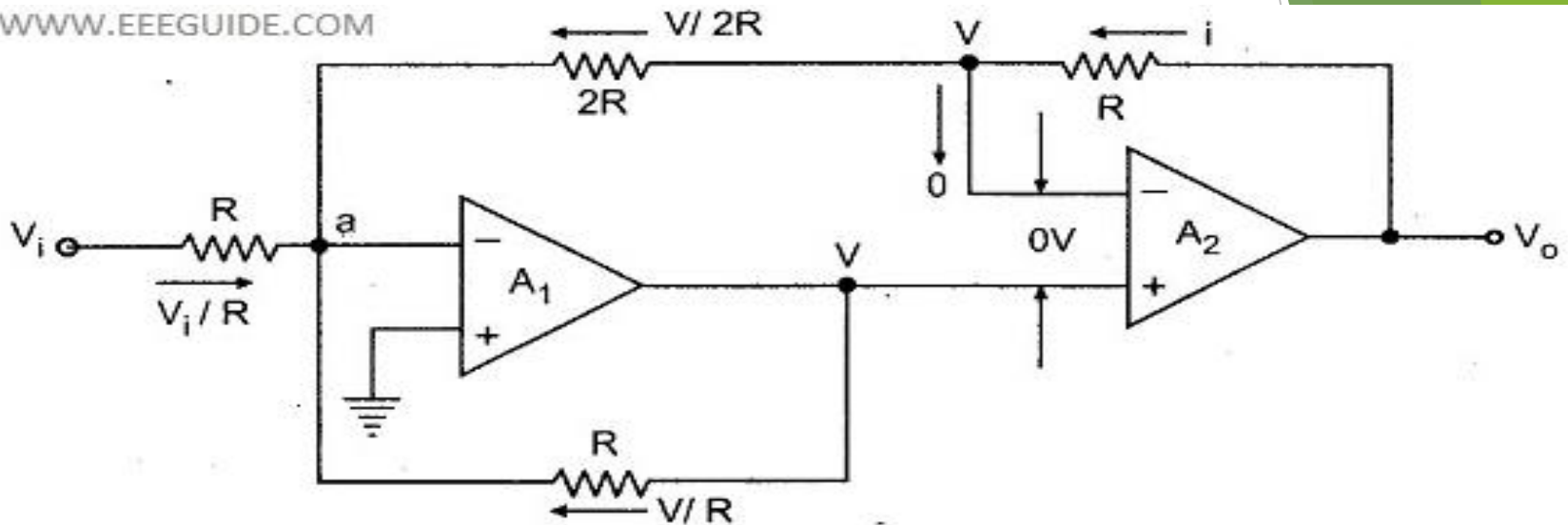
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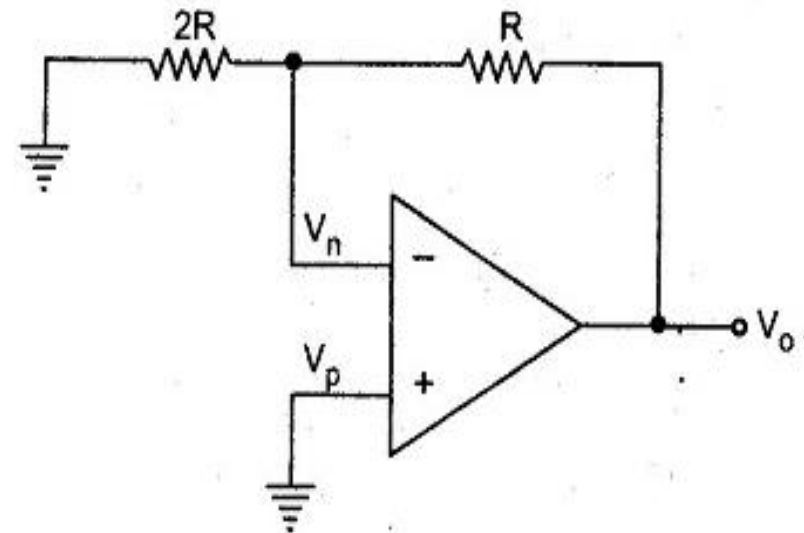
- ▶ When  $V_i < 0$ ,  $A_1$  is positive
- ▶  $D_1$ -RB,  $D_2$ -FB
- ▶ Eqwt circuit is as shown:

# Continued....

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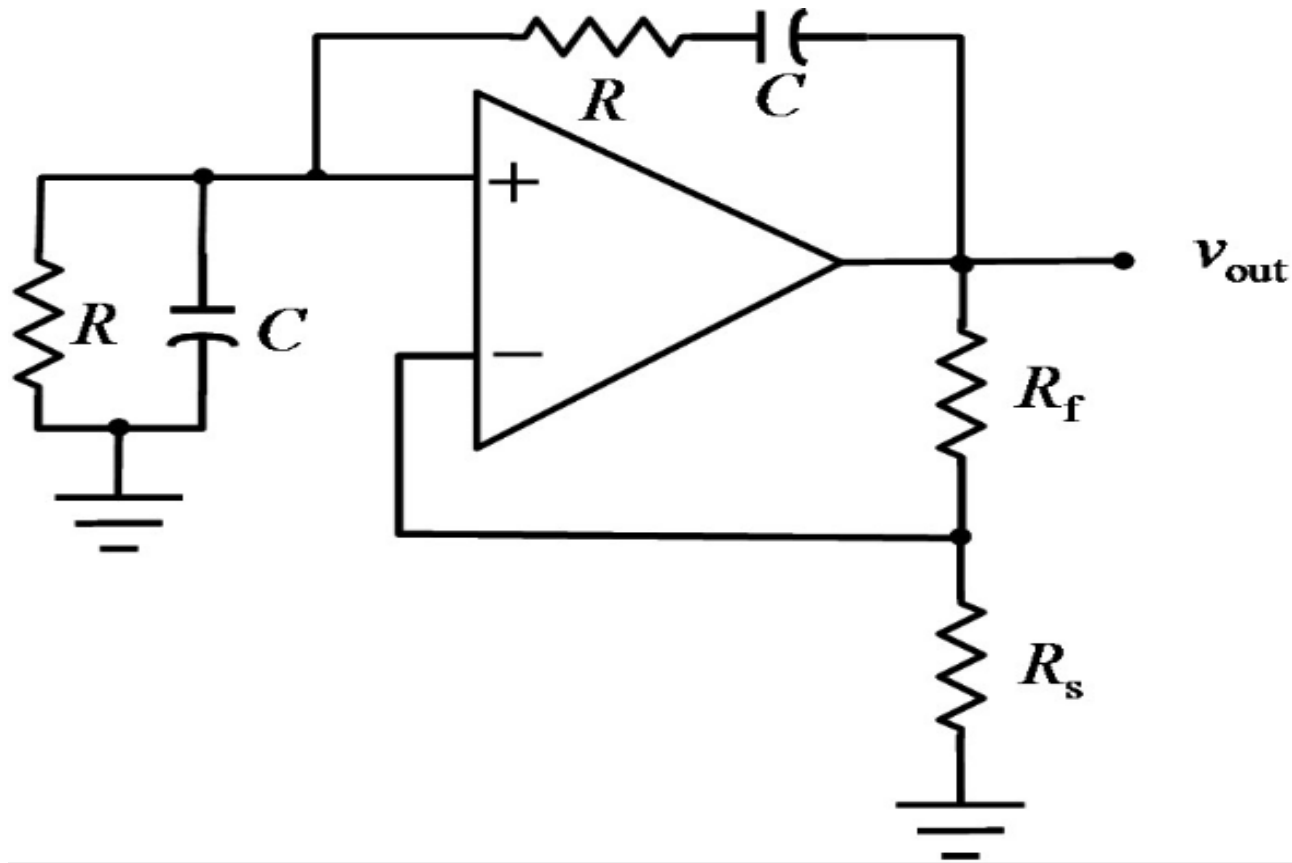


- ▶  $V_i/R + V/2R + V/R = 0$
- ▶  $V = -2/3 V_i$
- ▶  $V_o = (1 + R/2R)(-2/3 V_i) = -V_i$
- ▶ As  $V_i$  is negative,  $V_o$  is also negative
- ▶  $V_o = -V_i$





# WEIN BRIDGE OSCILLATOR



- ▶ AF oscillator
- ▶ Feedback circuit is a tank circuit which generates weak oscillations and it is amplified using an opamp.
- ▶ Here it works as a non inverting amplifier.
- ▶ Series impedance is denoted by  $Z_s$  and Parallel impedance is denoted by  $Z_p$

# Continued....

▶  $Z_s = R + X_c = R + \frac{1}{j\omega C} \dots\dots\dots 1$

▶  $Z_p = R X_c / R + X_c = \frac{R}{j\omega C} / R + \frac{1}{j\omega C} = \frac{R}{1 + j\omega RC} \dots\dots\dots 2$

▶  $V_f = \beta V_o \quad \beta = \frac{V_f}{V_o}$

▶  $\beta = \frac{Z_p}{Z_s + Z_p} = \frac{R}{1 + j\omega RC} / \left[ \left( R + \frac{1}{j\omega C} \right) + \frac{R}{1 + j\omega RC} \right]$

▶  $\left[ \frac{R}{1 + j\omega RC} \right] / \left[ \frac{j\omega RC + 1}{j\omega C} + \frac{R}{1 + j\omega RC} \right] = \left[ \frac{R}{1 + j\omega RC} \right] / \frac{(1 + j\omega RC)^2 + j\omega RC}{j\omega C(1 + j\omega RC)}$

▶  $\left[ \frac{R}{1 + j\omega RC} \right] \times \frac{j\omega C(1 + j\omega RC)}{(1 + j\omega RC)^2 + j\omega RC} = \frac{j\omega RC}{(1 + j\omega RC)^2 + j\omega RC} = \frac{j\omega RC}{1 + 3j\omega RC - (\omega RC)^2}$

▶ To ensure phase shift of 0 degree by the feedback network

▶  $1 - (\omega RC)^2 = 0$  (Equate real part to zero)

▶  $\omega = \frac{1}{RC} \quad f = \frac{1}{2\pi RC}$

▶ Equate imaginary part to 0

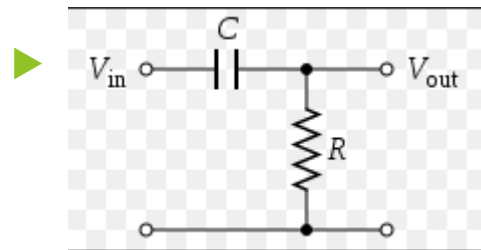
▶ feedback gain = 1/3

▶  $AB = 1$  then  $A = 3$ ; If  $A < 3$  damped oscillations ;  $A > 3$  growing oscillation

# RC PHASE SHIFT OSCILLATOR

- ▶ Amplifiers with positive feedback

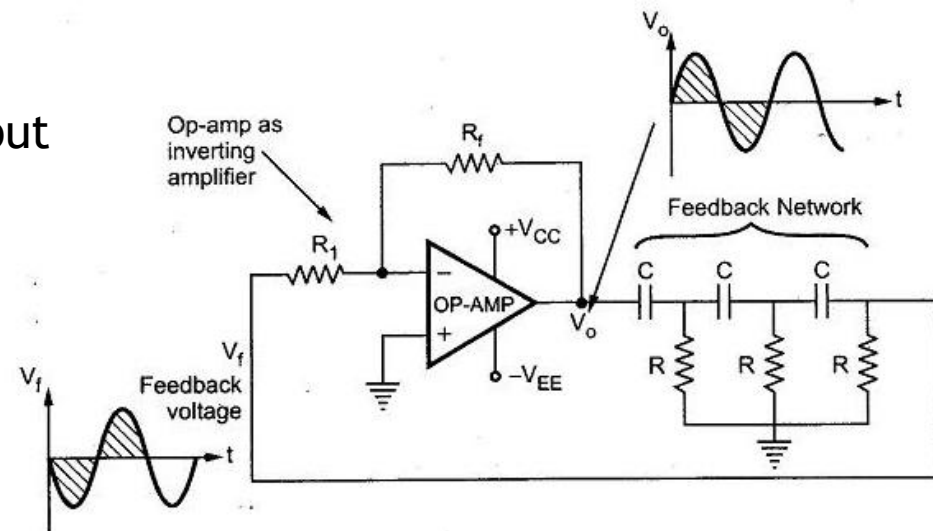
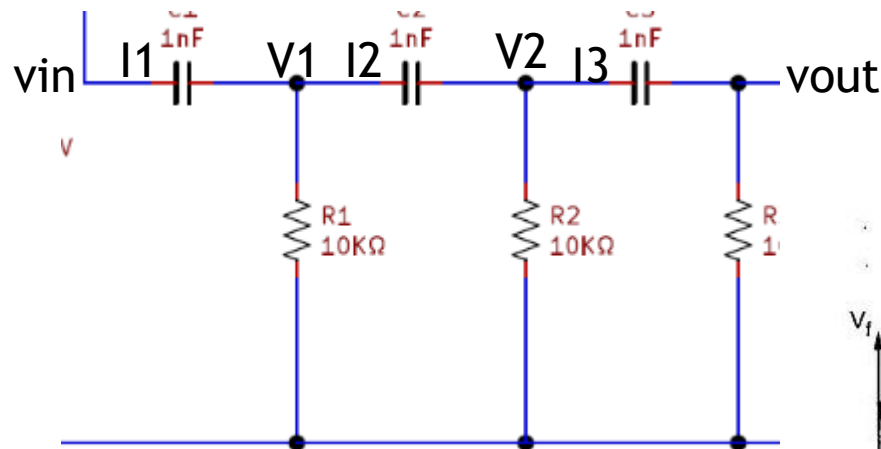
- ▶  $|AB|=1$   $\text{angle}(AB)=0$



$$\frac{V_o}{V_{in}} = \frac{R}{R - jX_C} = 1 / (1 - j \frac{X_C}{R})$$

- ▶  $\Phi = 0 - \tan^{-1} \left( -\frac{1}{\omega RC} \right) = \tan^{-1} \left( \frac{1}{\omega RC} \right) = \tan^{-1} \left( \frac{X_C}{R} \right)$

- ▶ If  $R=0$ ,  $\Phi=90$ degree(ideal) ;  $60$ degree(practical)



# Continued.....

► At node V2:

$$V_2 = I_3 X_c + V_o = \left(\frac{V_o}{R} X_c\right) + V_o = \frac{V_o}{j\omega RC} + V_o = V_o \left(1 + \frac{1}{j\omega RC}\right) \text{-----1}$$

At node V2 apply KCL,

$$I_2 = \frac{V_2}{R} + I_3 = \frac{V_o}{R} \left(1 + \frac{1}{j\omega RC}\right) + \frac{V_o}{R} = \frac{V_o}{R} \left(2 + \frac{1}{j\omega RC}\right) \text{-----2}$$

► At node V1:

$$V_1 = V_2 + I_2 X_c = V_o \left(1 + \frac{1}{j\omega RC}\right) + \frac{V_o}{j\omega CR} \left(2 + \frac{1}{j\omega RC}\right)$$

$$V_1 = V_o \left(1 + \frac{3}{j\omega RC} - \frac{1}{(\omega RC)^2}\right) \text{-----3}$$

At node V1 apply KCL,

$$\begin{aligned} I_1 &= \frac{V_1}{R} + I_2 = \frac{V_o}{R} \left(1 + \frac{3}{j\omega RC} - \frac{1}{(\omega RC)^2}\right) + \frac{V_o}{R} \left(2 + \frac{1}{j\omega RC}\right) \\ &= \frac{V_o}{R} \left(3 + \frac{4}{j\omega RC} - \frac{1}{(\omega RC)^2}\right) \text{-----4} \end{aligned}$$

At Vin:

$$\begin{aligned} V_{in} &= V_1 + I_1 X_c = V_o \left(1 + \frac{3}{j\omega RC} - \frac{1}{(\omega RC)^2}\right) + \frac{V_o}{j\omega RC} \left(3 + \frac{4}{j\omega RC} - \frac{1}{(\omega RC)^2}\right) \\ &= V_o \left[1 + \frac{6}{j\omega RC} - \frac{5}{(\omega RC)^2} - \frac{1}{j(\omega RC)^3}\right] \end{aligned}$$

# Continued.....

► Equate imaginary part to zero:

$$\frac{6}{wRC} - \frac{1}{(wRC)^3} = 0 \quad (wRC)^2 = \frac{1}{6} \quad w = \frac{1}{\sqrt{6}} * \frac{1}{RC}$$

$$f = \frac{1}{2\pi RC\sqrt{6}}$$

Questions:

1. With the help of circuit diagram and relevant equations, explain the disadvantages of a differentiator. How are the disadvantages removed in a practical differentiator?
2. With the help of circuit diagrams and graphs, explain the working of a Full wave Precision rectifier.
3. With the help of a circuit diagram, derive the equation for load current  $I_L$ , for a V to I converter with grounded load and deduce the condition for its ideal current converter
4. Derive the equation for frequency of oscillation ( $f_0$ ) of a Wein Bridge oscillator. Design a Wein Bridge oscillator for  $f_0 = 1\text{KHz}$ .
5. Draw the circuit of a log amplifier with temperature compensation and derive the equation for its output voltage

## Continued...

6. Derive the equation for output voltage of an integrator. Why is it called a lossy integrator?
7. Prove that the input voltage is converted into corresponding output current in a voltage to current converter with floating load
8. How to realize Wein-Bridge oscillator using op. amp.? Derive the condition of oscillation and frequency of oscillation for the circuit
9. Design a fullwave rectifier to rectify an ac signal of 0.2V peak-to-peak. Explain its principle of operation.