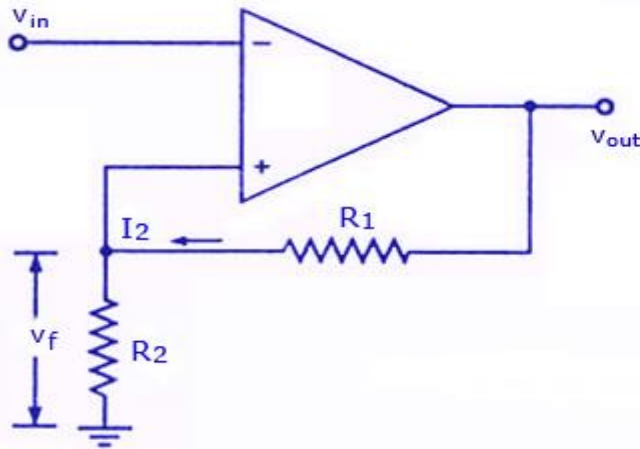


MODULE 4-ANALOG INTEGRATED CIRCUITS

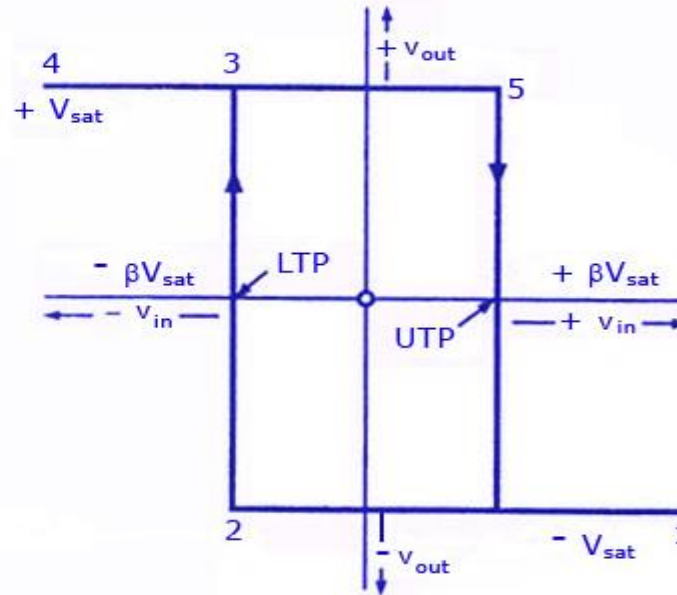
CREDITS-4

COURSE CODE: EC 204

SCHMITT TRIGGER USING OPAMP



(a) Circuit Diagram



(b) Input Output Characteristics

Schmitt Trigger

- Assume $V_{out}=+V_{sat}$, then input at non inverting terminal will be βV_{sat} where $\beta = \frac{R2}{R1+R2}$
- When voltage at inverting terminal will be less than V_f then $V_o=+V_{sat}$
- When voltage at inverting terminal will be greater than V_f then $V_o=-V_{sat}$
- Switching between $+V_{sat}$ and $-V_{sat}$ forms a square wave and thus squaring circuit works.

Continued....

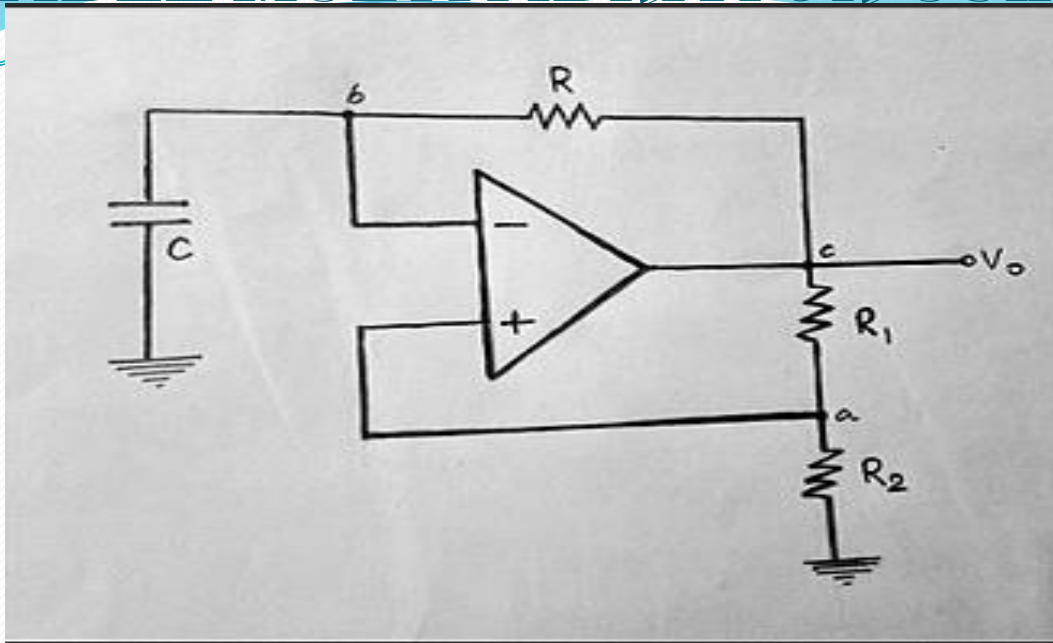
- If positive feedback is added to the comparator circuit ,gain can be increased.
- If the loop gain is unity,gain with feedback is infinite and transits between $-V_{sat}$ and $+V_{sat}$
- Also exhibits a phenomenon called hysteresis/backlash
- Input voltage triggers the o/p voltage V_o every time it exceeds certain voltage levels
- Voltage levels are Upper Threshold voltage(V_{ut}) and Lower Threshold voltage(V_{lt})
- Hysterisis width = $V_{ut}-V_{lt}=\beta V_{sat}-(-\beta v_{sat})=2\beta V_{sat}$

1. $R_1=50k\Omega, R_2=100\Omega, V_{ref}=0V, V_i=1V_{pp}, V_{sat}=+/-14V$. Determine V_{ut} and V_{lt}

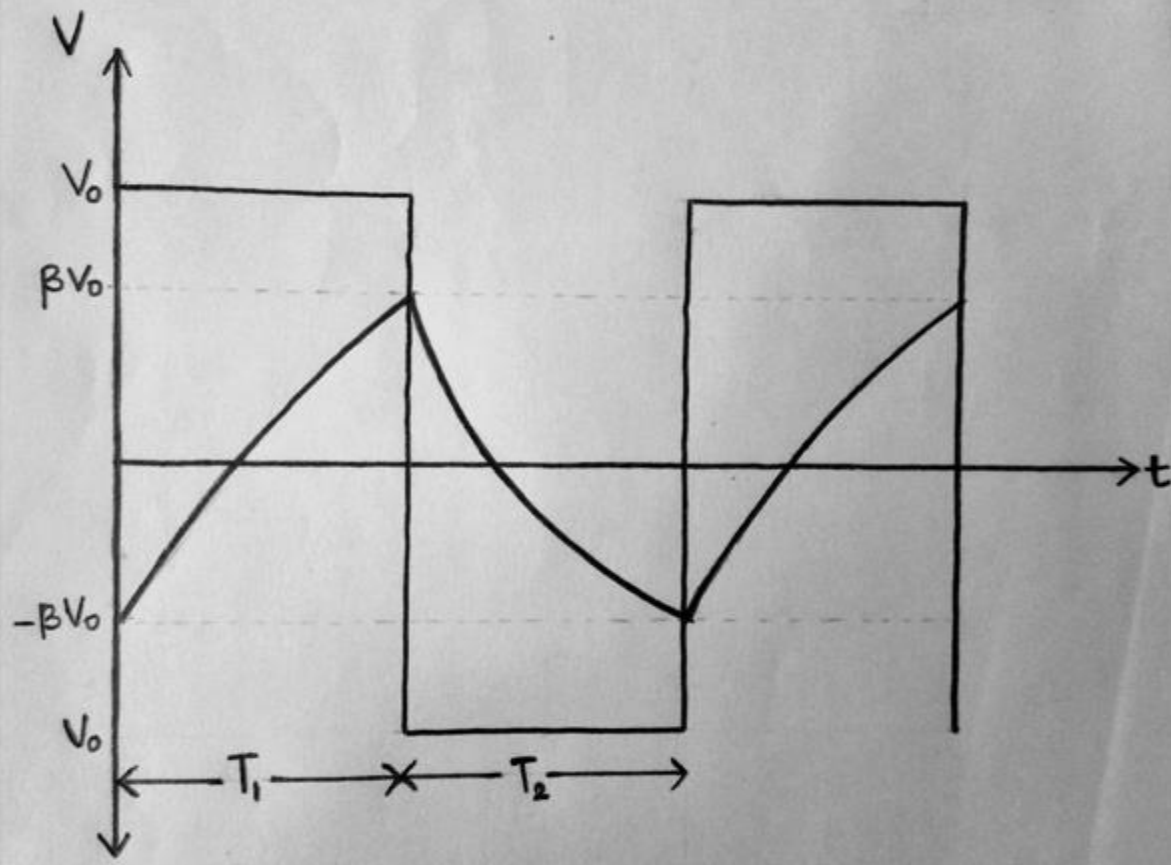
$$V_{ut}=\frac{100}{50100}*14=28mV$$

$$V_{lt}=\frac{100}{50100}* -14=-28mV$$

ASTABLE MULTIVIBRATOR USING OPAMP



- Assume $V_o = +V_{sat}$ voltage at non inverting terminal be βV_{sat} where $\beta = \frac{R_2}{R_1 + R_2}$
- At the same time capacitor charges through R . When voltage at the inverting terminal is less than βV_{sat} , o/p remains to be at $+V_{sat}$ and when voltage increases beyond βV_{sat} , o/p switches to $-V_{sat}$. Then the $V_+ = -\beta V_{sat}$
- At that time capacitor charges to $-V_{sat}$. o/p remains to be at $-V_{sat}$ until V_- is more negative than $-\beta V_{sat}$. When it becomes less negative than $-\beta V_{sat}$, o/p becomes $+V_{sat}$. Thus square waveform is generated.



- The period of the output waveform is determined by the RC time constant
- Time period : $T = 2RC \ln\left(\frac{1+\beta}{1-\beta}\right)$
- The frequency is determined by the time it takes the capacitor to charge from $-\beta V_{sat}$ to $+\beta V_{sat}$ and vice versa. The voltage across the capacitor as a function of time is given by,
- $V_c(t) = V_f + (V_i - V_f)e^{-\frac{t}{RC}}$

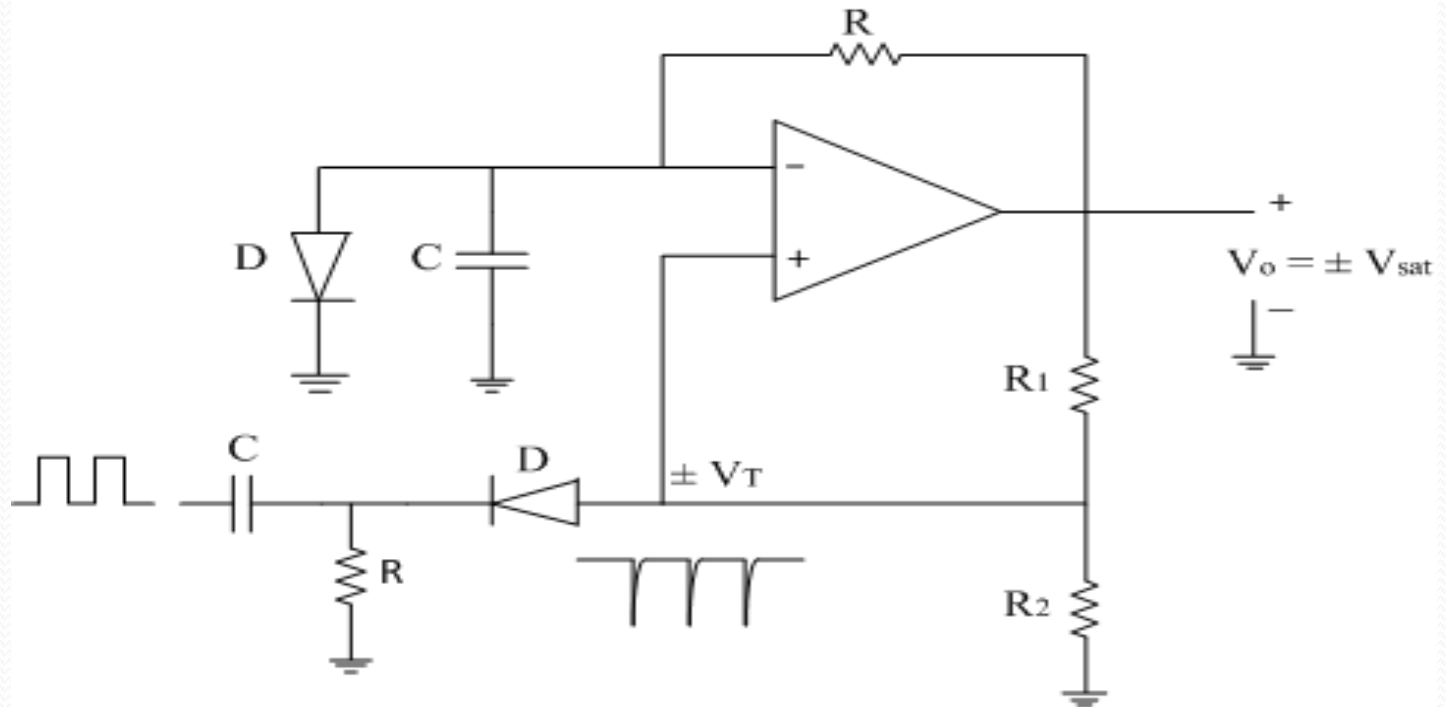
Continued....

- Final value, $V_f = +V_{sat}$ and initial value, $V_i = -\beta V_{sat}$
- $V_c(t) = V_{sat} - v_{sat}(1 + \beta) e^{\frac{-t}{RC}}$
- At $t = T_1$, voltage across the capacitor reaches βV_{sat} and switching takes place
- $\beta V_{sat} = V_{sat} - v_{sat}(1 + \beta) e^{\frac{-t}{RC}}$
- $T_1 = RC \ln\left(\frac{1 + \beta}{1 - \beta}\right)$ half of the period

$$T = 2T_1 = 2RC \ln\left(\frac{1 + \beta}{1 - \beta}\right)$$

MONOSTABLE MULTIVIBRATOR USING OPAMP

- One stable state and the other quasi stable



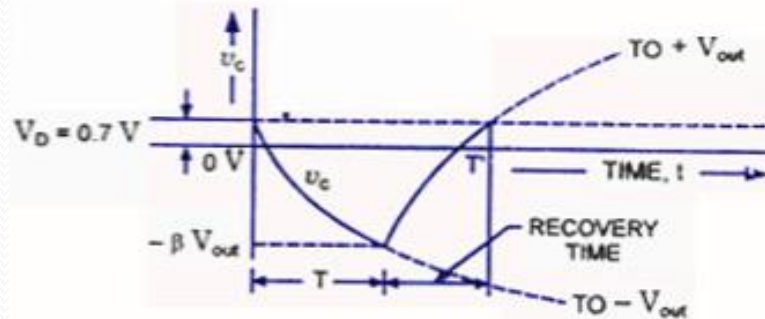
- If Diode clamps the capacitor voltage to $0.7V$ when the o/p is at $+V_{sat}$
- A pulse signal when passed through the differentiator RC and Diode provides negative going trigger to the $+$ input terminal.
- Assume $V_o = +V_{sat}$. Diode conducts and capacitor gets clamped to $0.7V$
- Voltage at non inverting terminal is $+\beta V_{sat} - V_1$
- If effective voltage is less than $0.7V$, o/p switches from $+V_{sat}$ to $-V_{sat}$.

Working continued....

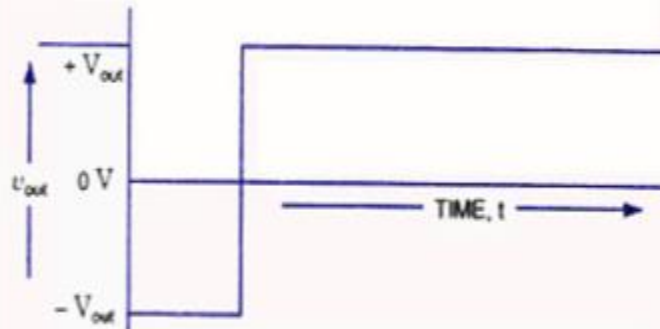
- Then the diode will be reverse biased and capacitor charges exponentially to $-V_{sat}$ through resistance R
- Voltage at the non inverting terminal be $-\beta V_{sat}$. When the capacitor voltage becomes slightly more negative than $-\beta V_{sat}$, o/p switches to $+V_{sat}$.



(b) Negative Trigger Pulse



(c) Waveform of v_c

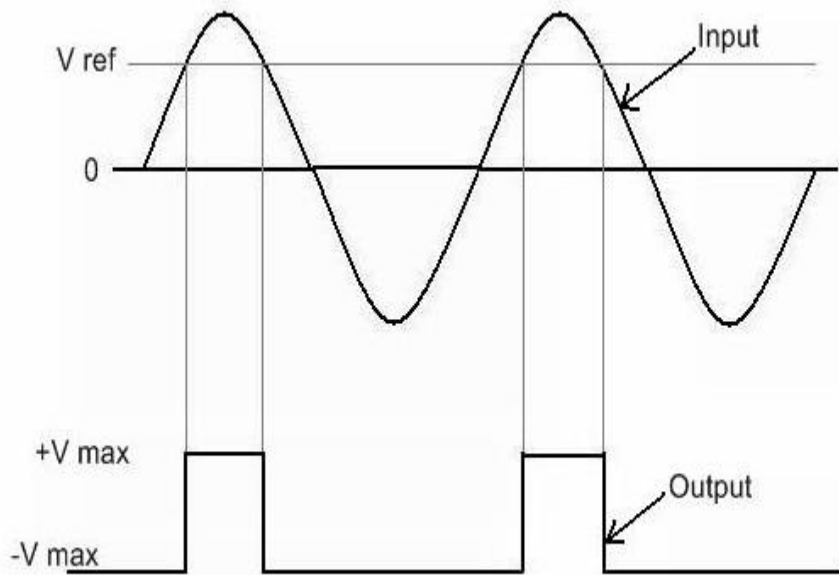


PULSEWIDTH

- $V_c(t) = V_f + (V_i - V_f) e^{\frac{-t}{RC}}$
- As $V_f = -V_{sat}, V_i = V_d$
- $V_c(t) = -V_{sat} + (V_d + V_{sat}) e^{\frac{-t}{RC}}$
- At $t = T, V_c(t) = -\beta V_{sat}$
- $-\beta V_{sat} = -V_{sat} + (V_d + V_{sat}) e^{\frac{-t}{RC}}$
- $e^{\frac{t}{RC}} = \frac{V_d + V_{sat}}{-\beta V_{sat} + V_{sat}} = \frac{V_{sat}(1 + V_d/V_{sat})}{V_{sat}(1 - \beta)}$
- $T = RC \ln \frac{(1 + V_d/V_{sat})}{(1 - \beta)}$ where $\beta = \frac{R_2}{R_1 + R_2}$
- If $V_{sat} \gg V_d$ and $R_1 = R_2$ so that $\beta = 0.5$ then
- $T = 0.69 RC$

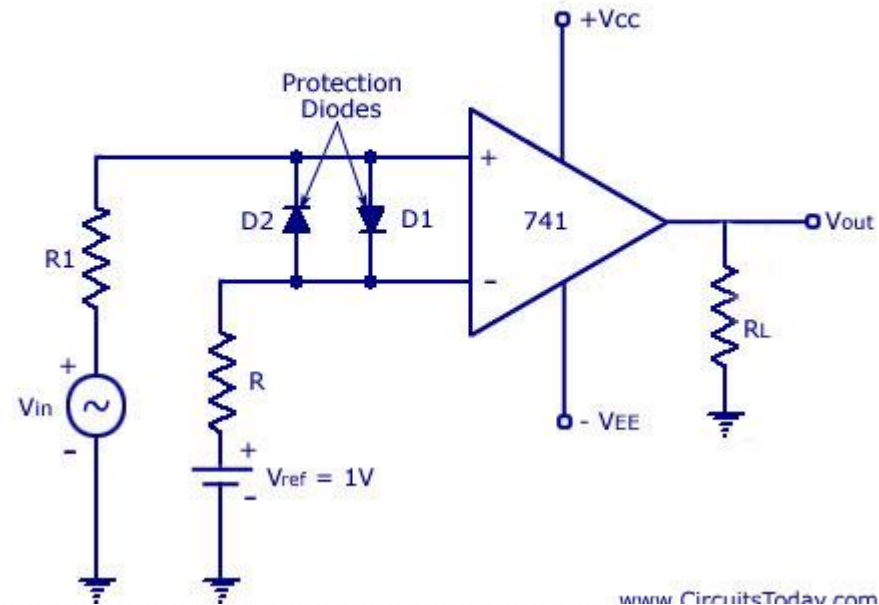
COMPARATORS

- Compares a signal voltage applied at one input of an opamp with a known reference voltage
- A reference voltage, V_{ref} is applied To -ve input and input is applied to +ve i/p.
- When $V_i < V_{ref}$ o/p voltage is $-V_{sat}$
- When $V_i > V_{ref}$, o/p voltage is $+V_{sat}$

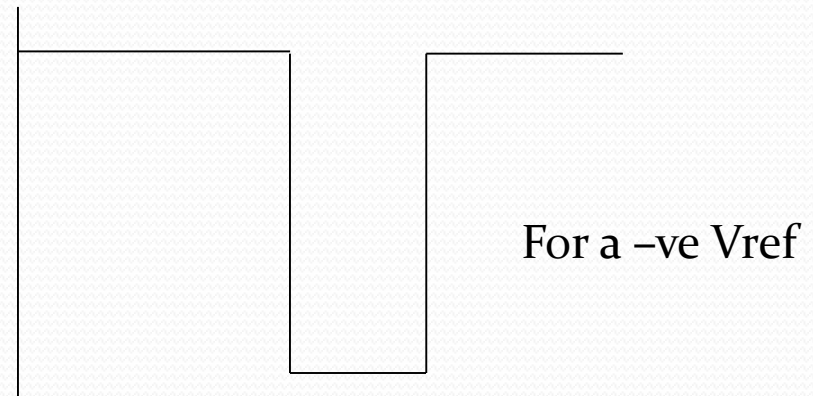


For a +ve V_{ref}

Non-Inverting Comparator Circuit



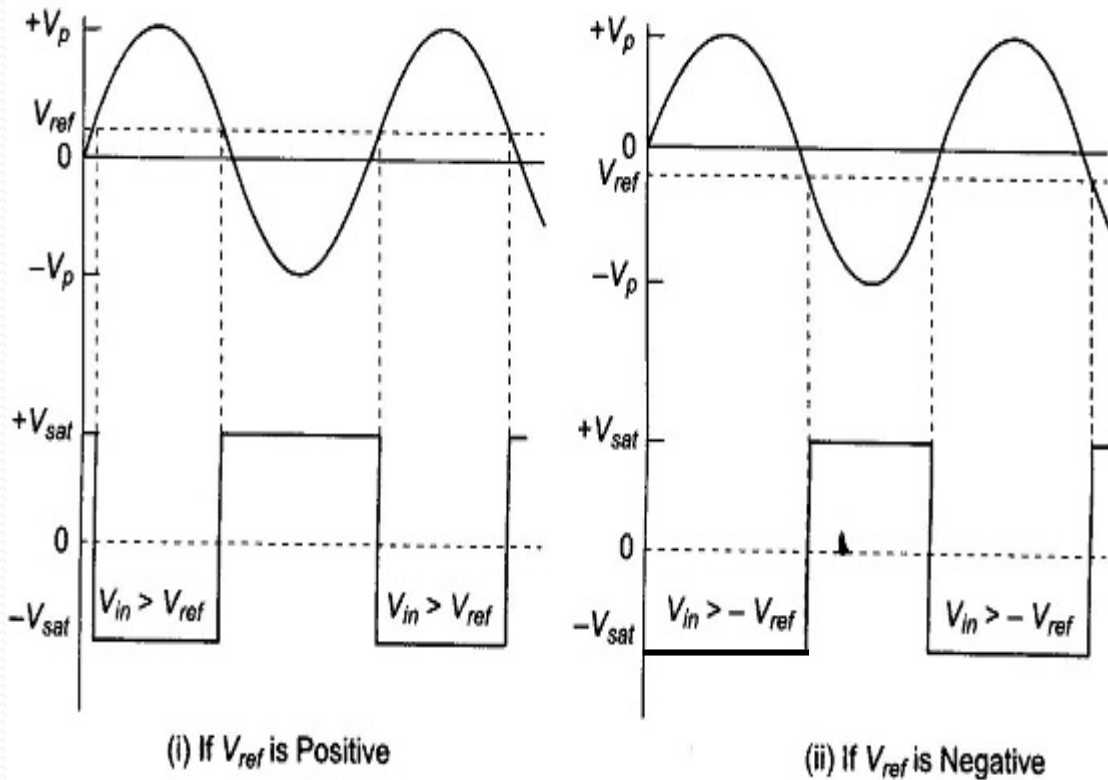
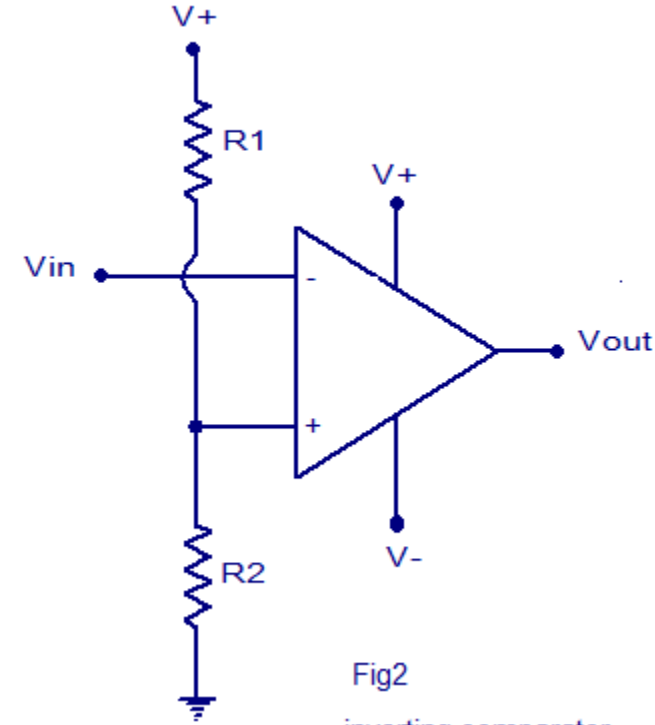
www.CircuitsToday.com



For a -ve V_{ref}

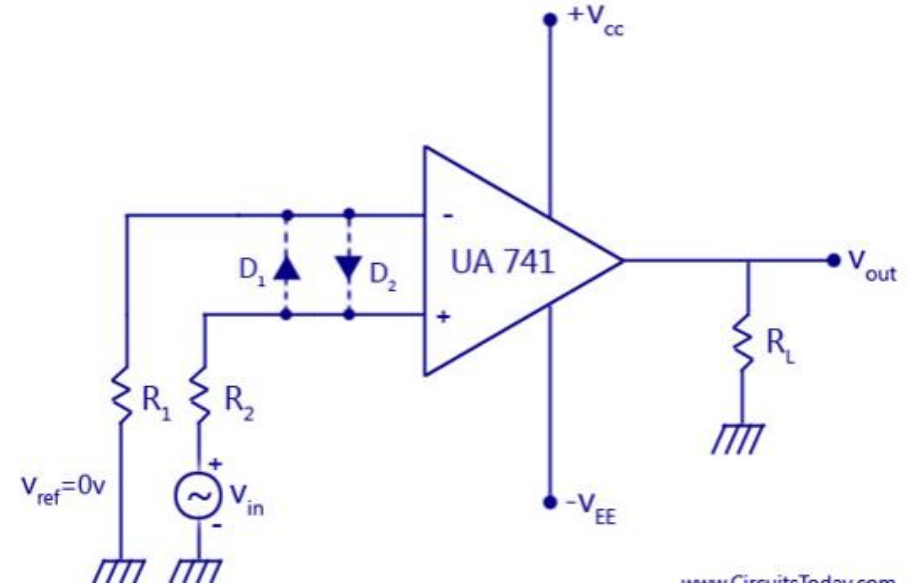
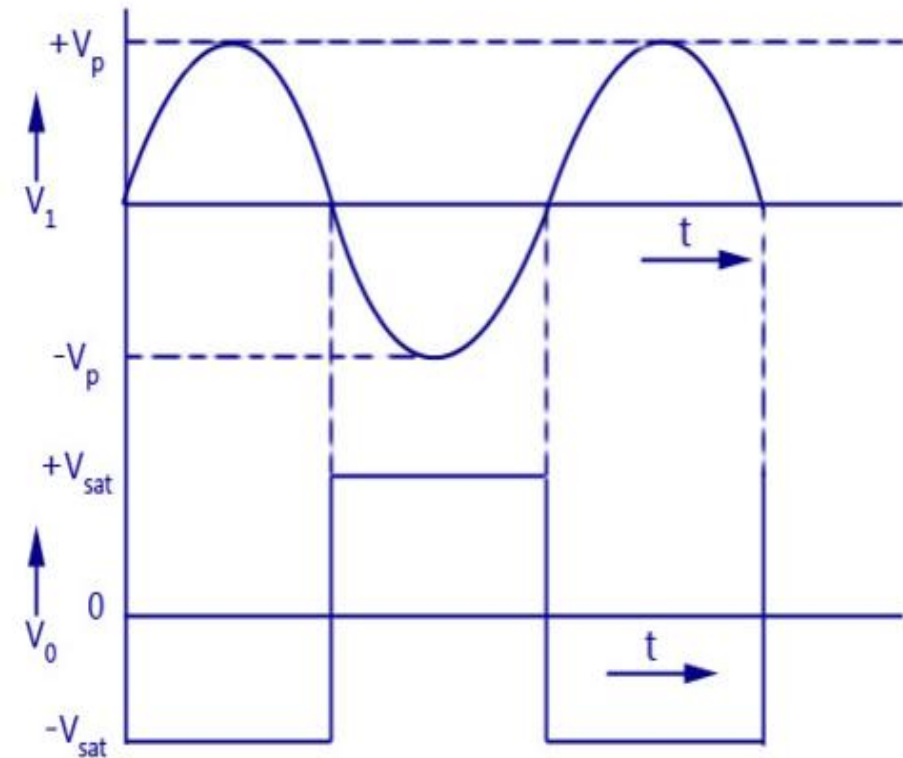
Continued.....

- V_{ref} is applied to the + input and V_{in} is
- Applied to the - input.
- When $V_i < V_{ref}$ o/p voltage is $+V_{sat}$
- When $V_i > V_{ref}$, o/p voltage is $-V_{sat}$



ZERO CROSSING DETECTOR

- V_{ref} is set to zero
- Sine to square wave generator
- V_{in} is applied to inverting i/p



TRIANGULAR WAVE GENERATOR

- Integrating a square wave

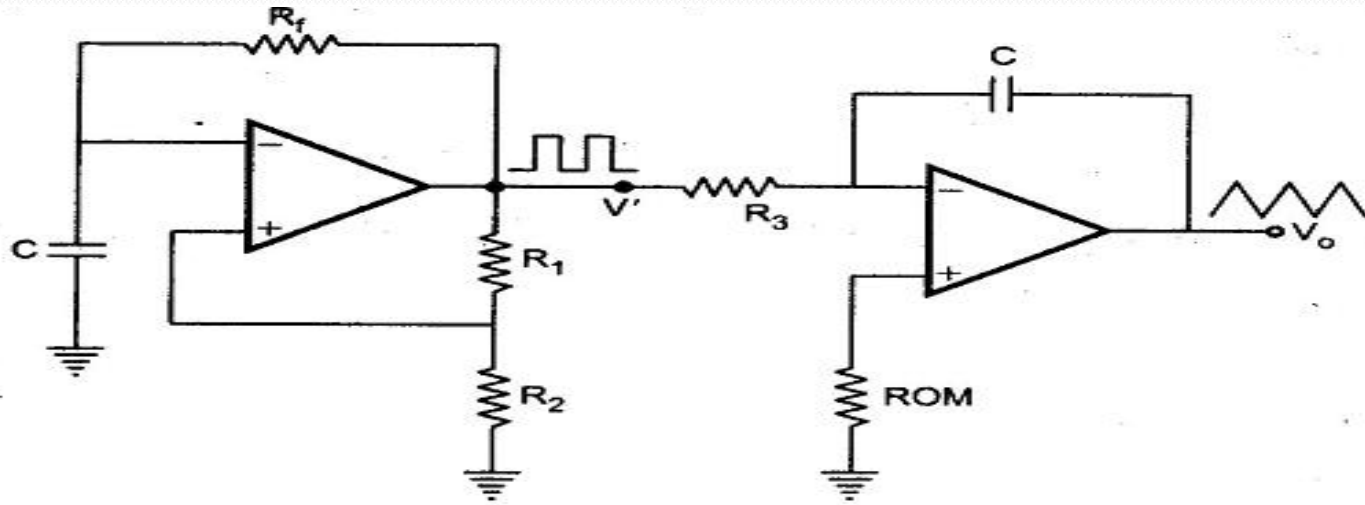
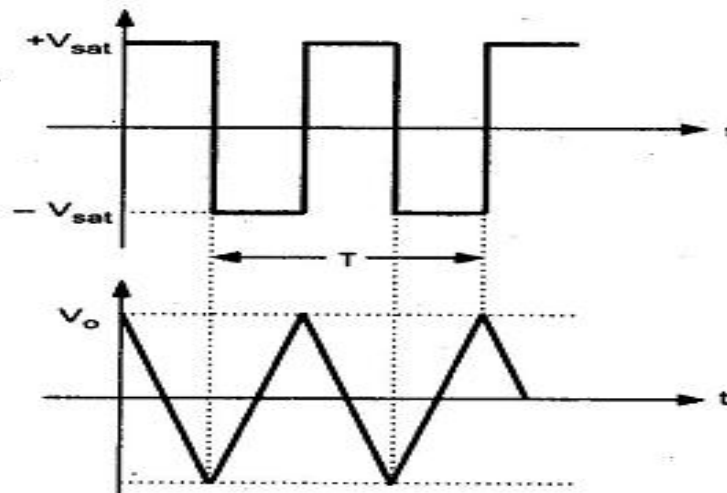
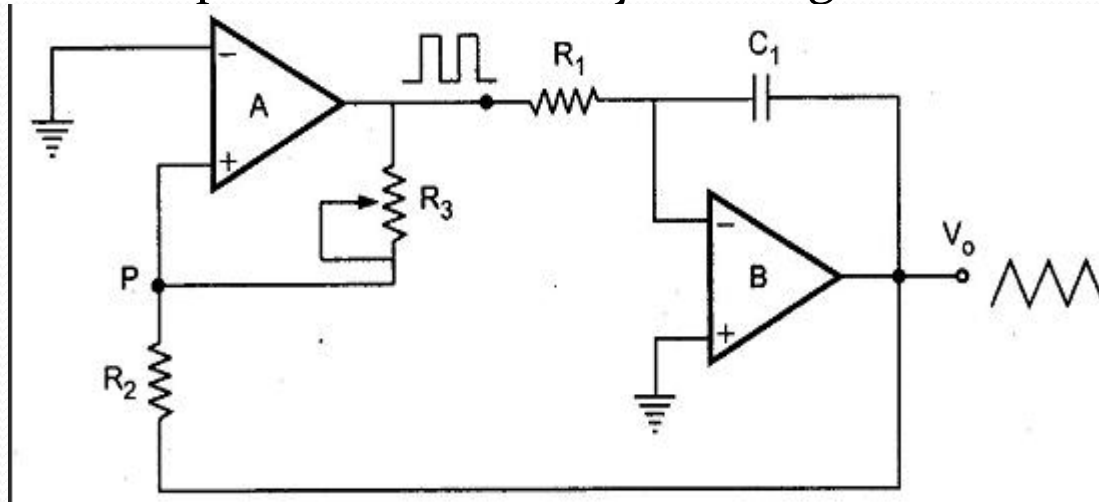


Fig. 2.85 Triangular wave generator



Alternate circuit

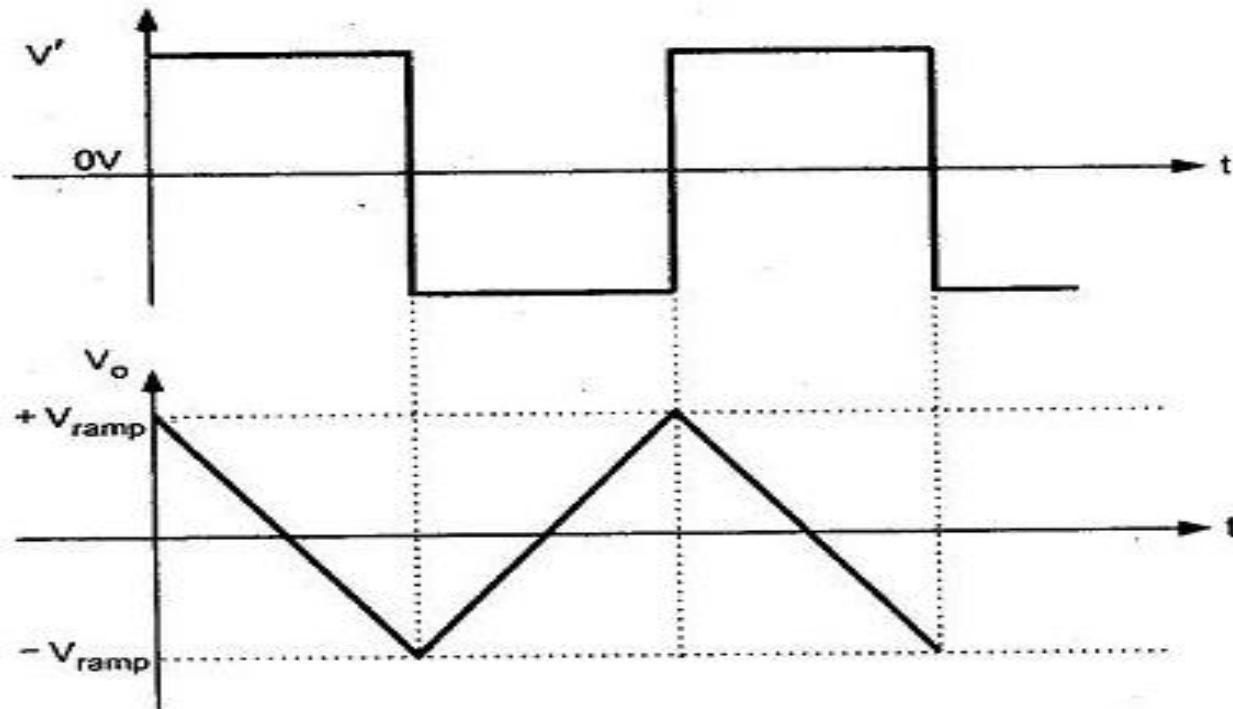
- Using lesser number of components
- Two level comparator followed by an integrator



- o/p of comparator A is a square wave of amplitude $\pm V_{sat}$ and is applied to $-ve$ input terminal of the integrator B producing a triangular wave.
- Triangular wave is fed back as input to the comparator A through a voltage divider R_2R_3
- Assume o/p of A is at $+V_{sat}$. o/p of integrator is $-ve$ going ramp
- One end of the voltage divider is at $+V_{sat}$ and other end at the negative going ramp of B.
- At time $t=t_1$, when the negative going ramp attains a value of $-V_{ramp}$, effective voltage at P becomes slightly less than $0V$. This switches o/p of A from $+V_{sat}$ to $-V_{sat}$.

Continued.....

- When o/p is at $-V_{sat}$, o/p of B increases to $+V_{ramp}$
- At time $t=t_2$, when the positive going ramp attains a value of $+V_{ramp}$, effective voltage at P becomes slightly above $0V$. This switches o/p of A from $-V_{sat}$ to $+V_{sat}$. Cycle repeats and forms a triangular waveform.
- Amplitude of the triangular wave depends upon RC value of the integrator B and o/p voltage level of A



FREQUENCY:

Effective voltage at P when the o/p of A is at +Vsat

$$-V_{ramp} + \frac{R_2}{R_2 + R_3} (+V_{sat} - (-V_{ramp}))$$

At $t=t_1$, voltage at point P = 0

$$-V_{ramp} + \frac{R_2}{R_2 + R_3} (+V_{sat} - (-V_{ramp})) = 0$$

$$-V_{ramp} + V_{ramp} \left(\frac{R_2}{R_2 + R_3} \right) + V_{sat} \left(\frac{R_2}{R_2 + R_3} \right) = 0$$

$$-V_{ramp} \left(\frac{R_3}{R_2 + R_3} \right) = -V_{sat} \left(\frac{R_2}{R_2 + R_3} \right)$$

$$-V_{ramp} = -V_{sat} \left(\frac{R_2}{R_3} \right) \text{-----1}$$

Effective voltage at P when the o/p of A is at -Vsat

$$V_{ramp} = V_{sat} \left(\frac{R_2}{R_3} \right) \text{-----2}$$

Peak to peak amplitude of the triangular wave, $V_o(p-p) = 2V_{sat} \left(\frac{R_2}{R_3} \right)$ --A

The time taken by the output to swing from $-V_{ramp}$ to $+V_{ramp}$ (or from $+V_{ramp}$ to $-V_{ramp}$) is equal to half the time period $T/2$.

Time can be calculated from the integrator o/p equation,

$$V_o(p-p) = \frac{-1}{R_1 C_1} \int_0^{T/2} (-V_{sat}) dt$$

$$= \frac{V_{sat}}{R_1 C_1} (T/2) \quad \text{or} \quad T = 2R_1 C_1 \frac{V_o(p-p)}{V_{sat}} \text{-----B}$$

Continued....

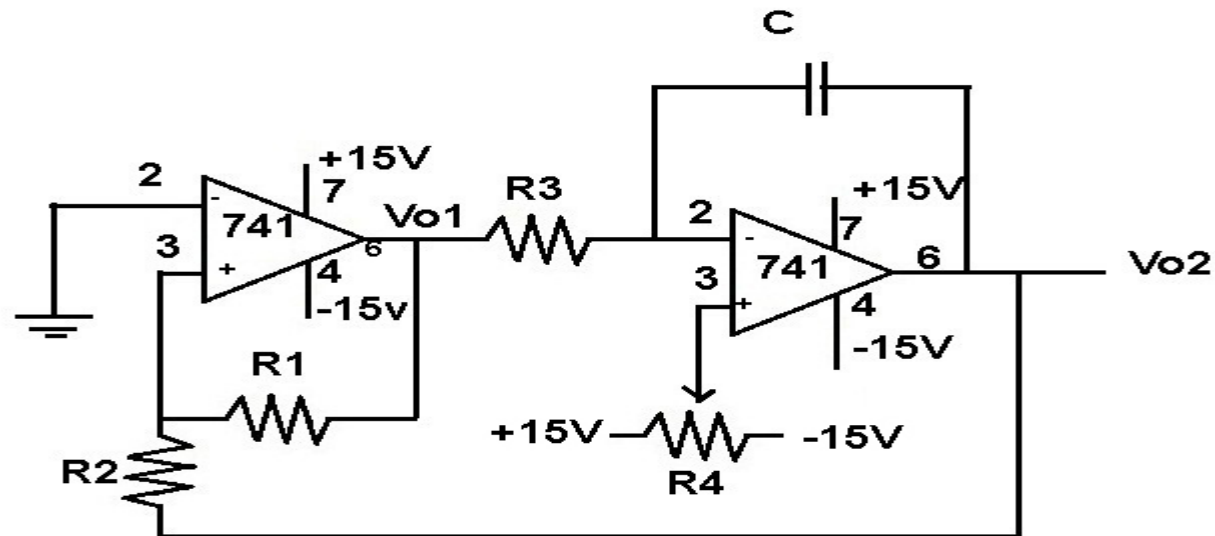
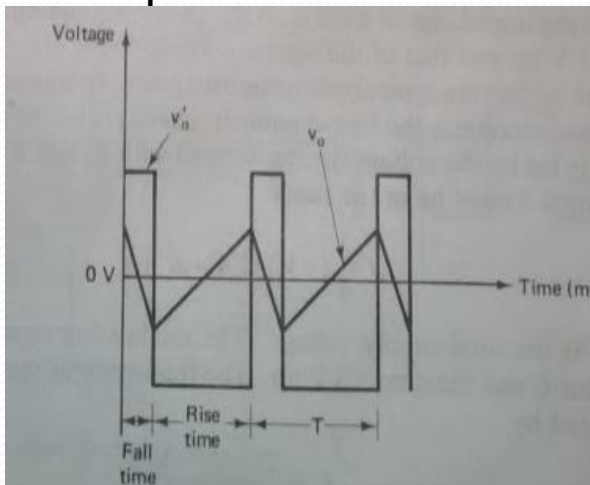
- Substitute A in B

$$T = \frac{4R_1R_2C_1}{R_3}$$

- Frequency of oscillation, $f = \frac{1}{T} = \frac{R_3}{4R_1R_2C_1}$

SAWTOOTH WAVEFORM GENERATOR:

- Sawtooth waveform can be also generated by an asymmetrical astable multivibrator followed by an integrator.
- The rise time of triangular wave is always equal to its fall of time. $t_r = t_f$
- For saw tooth generator, rise time may be much higher than its fall of time. $t_r > t_f$
- The triangular wave generator can be converted in to a saw tooth wave generator by injecting a variable dc voltage into the non-inverting terminal of the integrator.
- a potentiometer is used



FREQUENCY

$$f = \left(\frac{1}{RC} \right) \frac{V_i}{V_{ref}}$$

1. Design a sawtooth wave generator for 10V peak and frequency of 200Hz. Assume $V_i=2V$ and $V_{ref}=10V$

Ans: Let $R=10K\Omega$ $C=0.1\mu F$

$$F = \frac{1}{10 \times 10^3 \times 0.1 \times 10^{-6}} (2/10) = 200$$

2. Determine period, frequency, peak value of square wave, peak value of triangular wave. Assume $R_1=100K\Omega$, $R_2=10K\Omega$, $R_3=20K\Omega$, $C_1=0.01\mu F$, $V_{sat}=+/-14V$

$$\text{Ans: } T = \frac{4R_1R_2C_1}{R_3} = 2ms$$

$$f = 1/T = 500Hz$$

Peak value = +14V and -14 V

$$V_{ramp} = V_{sat} \left(\frac{R_2}{R_3} \right) = 7V$$

ACTIVE FILTERS

- Simplest way-Filter is made by using passive components(R,L,C)-which works for high frequencies.
- Active filters-opamp as active element + RLC as passive elements
- **Advantages:**
 - Increased current gain
 - No inductors-so reduction in size,weight and cost.
 - Reduction in parasitic capacitance.
 - Small cost
 - Rapid,stable and economical design of filters.
 - Easily tunable due to flexibility in gain and frequency adjustments.
 - High i/p impedance and low o/p impedance for opamp.So no loading effect and no need of buffer amplifier while cascading
 - Can realize rational function using active network
 - Eliminates passivity and reciprocity of RLC network
- **Limitations:**
 - High frequency response is limited by the gain-BW product and slew rate leading to lower BW
 - Large sensitivity(variation of filter parameter with supply voltage, temperature due to variation in gain of opamp, frequency response)
 - Requires dual polarity dc power supply.

FIRST ORDER LOWPASS FILTER

- Single RC network connected to the +terminal of non inverting opamp
- R_1 and R_f determine the gain of the filter in pass band.

Voltage across the capacitor C (s-domain

$$V_1(s) = \frac{1}{\frac{1}{sC} + R} V_{in}(s) \quad [V_{in} * X_C / R + X_C = V_1]$$

$$\frac{V_1(s)}{V_{in}(s)} = \frac{1}{RCs + 1} \quad \text{---1}$$

$$\text{Closed loop gain } A = [(1 + R_f/R_1)] = \frac{V_o(s)}{V_1(s)} \quad \text{---2}$$

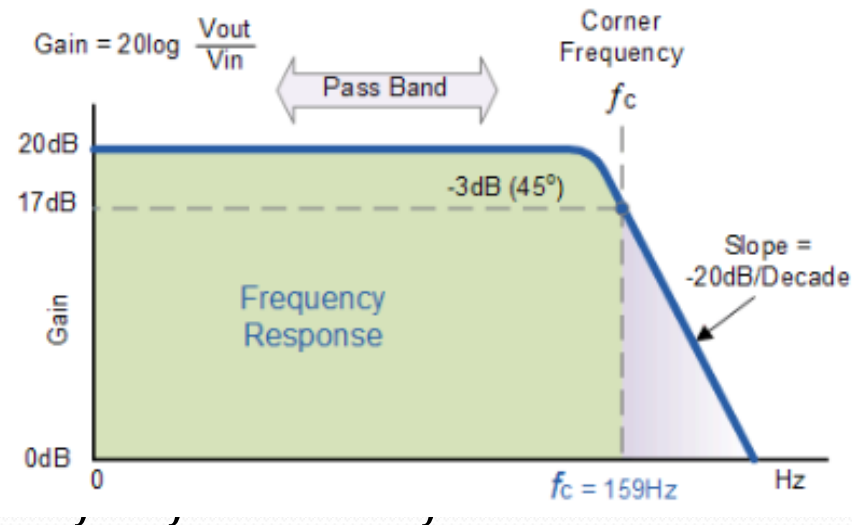
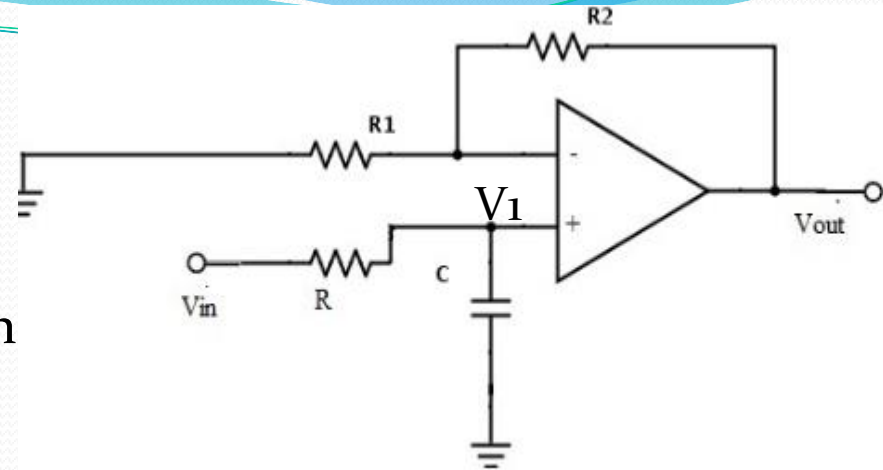
$$\text{Overall TF} = \frac{A}{RCs + 1} \quad \text{---3}$$

$$\text{Let } wh = \frac{1}{RC}$$

$$\text{Overall TF} = \frac{Awh}{s + wh} \quad \text{--- } T_1$$

Put $s = j\omega$ in 3

$$H(j\omega) = \frac{A}{RCj\omega + 1} = \frac{A}{1 + j\frac{\omega}{wh}} = \frac{A}{1 + j\frac{f}{f_h}} \quad \text{where } f = \frac{1}{2\pi RC} \text{ and } f = \frac{\omega}{2\pi}$$



Continued.....

- At very low frequency, $f \ll f_h$, $|H(j\omega)| \approx A$ (pass band)
- At $f = f_h$, $|H(j\omega)| = \frac{A}{\sqrt{2}} = 0.707A$ (-3dB down)
- At $f \gg f_h$, $|H(j\omega)| \ll A \approx 0$ (gain decreases at a rate of -20dB/decade-stop band)
- $A(s) = \frac{1}{s+1} = \frac{1}{j\omega+1} = \frac{1}{\sqrt{1+\omega^2}}$; $A(\text{dB}) = 20 \log 1 - 20 \log \sqrt{1+\omega^2}$; when $\omega=1$ $0 - 20 \log \sqrt{2} = -3\text{dB}$

LOW PASS FILTER DESIGN:

1. Choose the value of high cut off frequency, f_h
2. Select the value of capacitor C such that its value $\leq 1\mu\text{F}$
3. When the values f_h and C are known, the value of R can be calculated by using

$$f_h = \frac{1}{2\pi RC}$$

4. Finally select the values of R_i and R_f depending on the desired pass band gain by using $A = 1 + (R_f/R_1)$

1. Design a first order LPF at a cut-off frequency of 2KHz with a gain of 2.

Ans: $f_h = 2\text{KHz}$, $A = 2$

$$\text{Let } C = 0.01\mu\text{F}, \quad f = \frac{1}{2\pi RC}, \quad R = \frac{1}{2\pi f C} = \frac{1}{2\pi * 2 * 10^3 * 0.01 * 10^{-6}} = 7.95\text{k}\Omega$$

$$A = 1 + (R_f/R_1) = 2; \quad R_f = R_1 = 10\text{k}\Omega$$

SECOND ORDER LOWPASS FILTER(SALLEN-KEY)

- For 2nd order, $-20\log\sqrt{1 + (\frac{w}{w_0})^4} = -20\log(\frac{w}{w_0})^2 = -40\text{dB/dec}$

- Consists of 2 RC pairs and

Has a roll off rate of -40dB/decade

Due to virtual ground concept $V_{out} \approx V_b$

Apply KCL to node A

$$V_i Y_1 = V_a(Y_1 + Y_2 + Y_3) - V_o Y_3 - V_b Y_2$$

$$V_i Y_1 = V_a(Y_1 + Y_2 + Y_3) - V_o Y_3 - V_o \frac{Y_2}{A_0} \quad (\text{as } V_b * A_0 = V_o) \text{-----1}$$

Apply KCL to node B

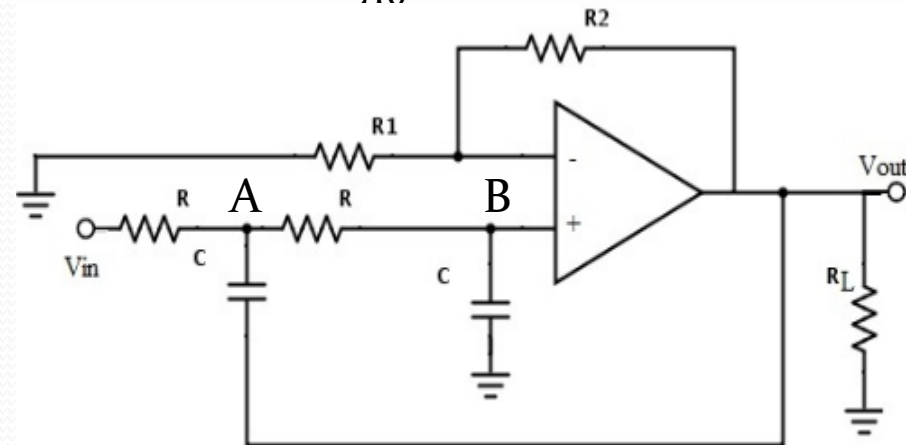
$$V_a Y_2 = V_b(Y_2 + Y_4) = \frac{V_o}{A_0}(Y_2 + Y_4)$$

$$V_a = V_o \frac{Y_2 + Y_4}{A_0 Y_2} \text{-----2}$$

Substitute 2 in 1 Gen:equation

$$\frac{V_o}{V_i} = \frac{A_0 Y_1 Y_2}{Y_1 Y_2 + Y_4(Y_1 + Y_2 + Y_3) + Y_2 Y_3(1 - A_0)}$$

To make a LPF, $Y_1 = Y_2 = 1/R, Y_3 = Y_4 = sC$

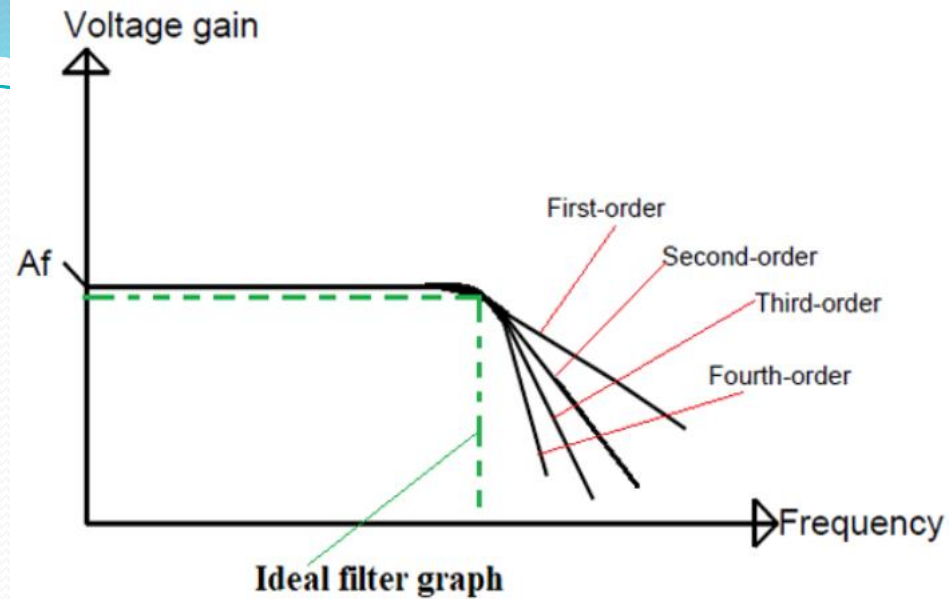


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- From 3, $H(s) = \frac{A_o}{(sCR)^2 + sCR(3-A_o) + 1}$ -----4
- $H(0) = A_o$ and $H(\infty) = 0$ Thus LPF is clear
- TF of 2nd order LPF, $H(s) = \frac{A_o \omega_h^2}{s^2 + \alpha \omega_h s + \omega_h^2}$ -----5 where $A_o = \text{gain}$, $\omega_h = \text{upper cut off frequency}$, $\alpha = \text{damping coefficient}$
- Compare 4 and 5 $\frac{A_o \omega_h^2}{s^2 + \alpha \omega_h s + \omega_h^2} = \frac{A_o}{(sCR)^2 + sCR(3-A_o) + 1}$
- $\omega_h = \frac{1}{RC}$ $\alpha = 3 - A_o$
- Value of the damping coefficient can be determined by the value of A_o
- Put $s = j\omega$ in 5
- Thus normalized frequency $s = j\left(\frac{\omega}{\omega_h}\right)$
- In dB, $|H(j\omega)| = 20 \log \frac{A_o}{\sqrt{\left(1 - \frac{\omega^2}{\omega_h^2}\right)^2 + \left(\alpha \frac{\omega}{\omega_h}\right)^2}}$
- Heavily damped filter, $\alpha > 1.7$, response is stable
- When α decreases, response exhibits overshoot and ripple at early stage
- If α is reduced too much, filter becomes oscillatory
- For $\alpha = 1.414$, flattest pass band occurs - **BUTTERWORTH FILTER** Eg: Audio filters
- For $\alpha = 1.06$ - Chebyshev filters and $\alpha = 1.73$ - Bessel filters

Continued....

- $|H(j\omega)|$ in dB = $20 \log \frac{A_0}{\sqrt{1 + (\frac{\omega}{\omega_h})^4}}$
- For nth order, $|H(j\omega)| = \frac{1}{\sqrt{1 + (\frac{\omega}{\omega_h})^{2n}}}$



| n (order) | Normalized Denominator Polynomials in Factored Form |
|-----------|--|
| 1 | $(1+s)$ |
| 2 | $(1+1.414s+s^2)$ |
| 3 | $(1+s)(1+s+s^2)$ |
| 4 | $(1+0.765s+s^2)(1+1.848s+s^2)$ |
| 5 | $(1+s)(1+0.618s+s^2)(1+1.618s+s^2)$ |
| 6 | $(1+0.518s+s^2)(1+1.414s+s^2)(1+1.932s+s^2)$ |
| 7 | $(1+s)(1+0.445s+s^2)(1+1.247s+s^2)(1+1.802s+s^2)$ |
| 8 | $(1+0.390s+s^2)(1+1.111s+s^2)(1+1.663s+s^2)(1+1.962s+s^2)$ |
| 9 | $(1+s)(1+0.347s+s^2)(1+s+s^2)(1+1.532s+s^2)(1+1.879s+s^2)$ |
| 10 | $(1+0.313s+s^2)(1+0.908s+s^2)(1+1.414s+s^2)(1+1.782s+s^2)(1+1.975s+s^2)$ |

- Design a second order Butterworth LPF having upper cut off frequency 1 KHz

$$f_h = \frac{1}{2\pi RC}; \alpha = 3 - A_0$$

$$\text{Let } C = 0.1\mu\text{F} \quad R = \frac{1}{2\pi f_h C} = \frac{1}{2\pi \cdot 1000 \cdot 0.1 \cdot 10^{-6}} = 1.6\text{K}\Omega$$

As Butterworth filter for order, $n=2$ then $\alpha=1.414$

$$A_0 = 3 - \alpha = 3 - 1.414 = 1.586$$

$$\text{TF} = \frac{1.586}{s^2 + 1.414s + 1} \quad (\text{denominator from the table})$$

$$A_0 = 1 + \frac{R_f}{R_i} = 1.586$$

So $R_f = 0.586R_i$ Let $R_f = 5.86\text{K}\Omega$ and $R_i = 10\text{K}\Omega$

Draw the circuit and mark the component values

- Design a fourth order Butterworth LPF having upper cut off frequency 1kHz

$$f_h = \frac{1}{2\pi RC}; \alpha = 3 - A_0$$

$$\text{Let } C = 0.1\mu\text{F} \quad R = \frac{1}{2\pi f_h C} = \frac{1}{2\pi \cdot 1000 \cdot 0.1 \cdot 10^{-6}} = 1.6\text{K}\Omega$$

$\alpha_1 = 0.765$, $\alpha_2 = 1.848$ two damping factors

$$A_{01} = 3 - \alpha_1 = 3 - 0.765 = 2.235$$

$$A_{02} = 3 - \alpha_2 = 3 - 1.848 = 1.152$$

$$\text{TF} = \frac{2.235}{s^2 + 0.765s + 1} \cdot \frac{1.152}{s^2 + 1.848s + 1}$$

$$A_{01} = 1 + \frac{R_f}{R_i} = 2.235 \quad \text{so } R_f = 1.235R_i \quad \text{Let } R_f = 12.35\text{K}\Omega \quad \text{and } R_i = 10\text{K}\Omega$$

$$A_{02} = 1 + \frac{R_f}{R_i} = 1.152 \quad \text{so } R_f = 0.152R_i \quad \text{Let } R_f = 15.2\text{K}\Omega \quad \text{and } R_i = 100\text{K}\Omega$$

Draw two second order LPF cascaded with R and C for both

1st stage $R_f = 12.35\text{K}\Omega$ and $R_i = 10\text{K}\Omega$

2nd stage $R_f = 15.2\text{K}\Omega$ and $R_i = 100\text{K}\Omega$

HIGH PASS ACTIVE FILTER

- Interchanging R and C in LPF

$$\frac{V_o}{V_i} = \frac{A_o Y_1 Y_2}{Y_1 Y_2 + Y_4 (Y_1 + Y_2 + Y_3) + Y_2 Y_3 (1 - A_o)}$$

Put $Y_1 = Y_2 = sC, Y_3 = Y_4 = 1/R$

$$H(s) = \frac{A_o s^2}{s^2 + (3 - A_o) \omega s + \omega^2}$$

where $\omega = \frac{1}{RC}$

$H(0) = 0$ and $H(\infty) = A_o$ Thus HPF is clear

$$|H(j\omega)| = \frac{A_o}{\sqrt{1 + (\frac{f}{f_c})^4}}$$

For nth order, $|H(j\omega)| = \frac{1}{\sqrt{1 + (\frac{f}{f_c})^{2n}}}$

- Design a second order Butterworth HPF having lower cut off frequency 1 KHz

$$f_c = \frac{1}{2 * \pi * RC} ; \alpha = 3 - A_o$$

Let $C = 0.1 \mu F$ $R = \frac{1}{2 * \pi * f_c * C} = \frac{1}{2 * \pi * 1000 * 0.1 * 10^{-6}} = 1.6 K \Omega$

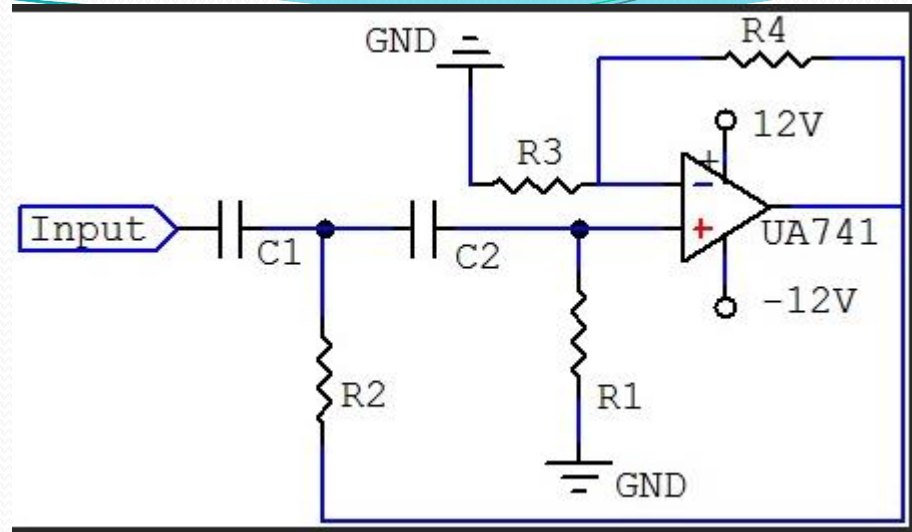
As butterworth filter for order, $n = 2$ then $\alpha = 1.414$

$$A_o = 3 - \alpha = 3 - 1.414 = 1.586$$

$$TF = \frac{1.586}{s^2 + 1.414s + 1} \text{ (denominator from the table)}$$

$$A_o = 1 + \frac{R_f}{R_i} = 1.586$$

So $R_f = 0.586 R_i$ Let $R_f = 5.86 K \Omega$ and $R_i = 10 K \Omega$



BAND PASS FILTER

- Depending on figure of merit and quality factor, there are two types :Narrow($Q > 10$) and Wide BPF($Q < 10$)

- $Q = \frac{f_0}{BW} = \frac{f_0}{f_h - f_l}$ and $f_0 = \sqrt{f_h f_l}$ where f_0 -central frequency

- **NARROW BANDPASS FILTER:**

- Important parameters are upper and lower cut off frequencies, Band width central frequency gain A_0 and selectivity Q

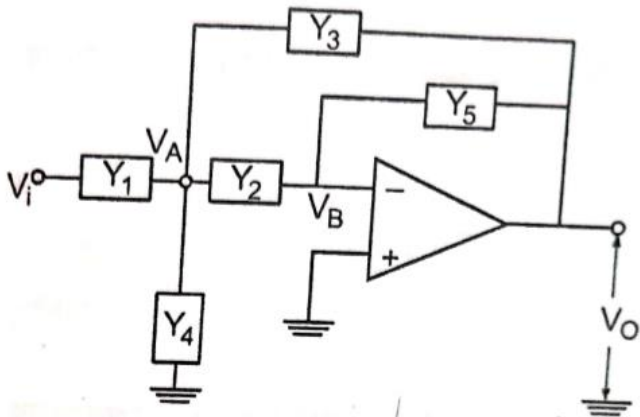


Fig.3.39 Band pass configuration

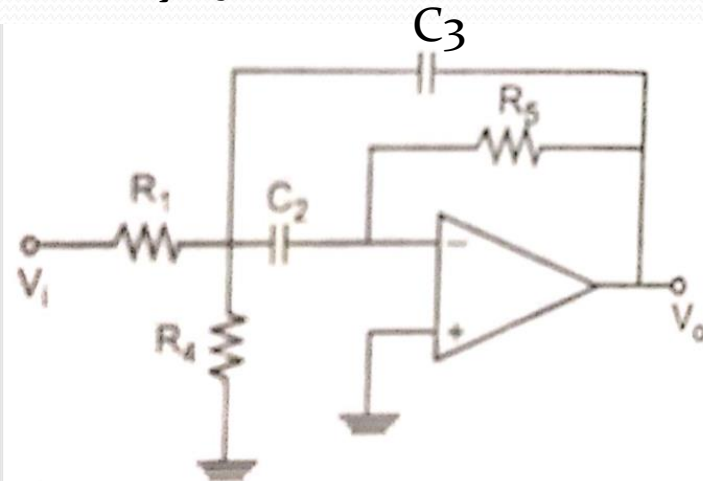


Fig.3.40 Second order band pass filter

- $Y_1 = G_1; Y_2 = sC_2 = Y_3 = sC_3; Y_4 = G_4; Y_5 = G_5$ -----A

- Apply KCL at node A,

$$(V_i - V_A)Y_1 = (V_A - 0)Y_4 + (V_A - V_B)Y_2 + (V_A - V_O)Y_3$$

$$V_B = 0 \text{ (virtual ground)}$$

$$V_i Y_1 + V_O Y_3 = V_A (Y_1 + Y_2 + Y_3 + Y_4) \text{-----1}$$

Continued.....

- Apply KCL at node B

$$(V_a - V_b)Y_2 = (V_b - V_o)Y_5 \quad V_b = 0$$

$$V_a Y_2 = -V_o Y_5 \quad V_a = -V_o \frac{Y_5}{Y_2} \quad \text{-----2}$$

Put V_a in eqn 1

$$V_i Y_1 + V_o Y_3 = -V_o \frac{Y_5}{Y_2} (Y_1 + Y_2 + Y_3 + Y_4)$$

$$V_i Y_1 = -V_o \left[\frac{Y_5 Y_1}{Y_2} + \frac{Y_5 Y_2}{Y_2} + \frac{Y_5 Y_3}{Y_2} + \frac{Y_5 Y_4}{Y_2} + \frac{Y_3 Y_2}{Y_2} \right]$$

$$V_i Y_1 = -V_o \left[\frac{Y_5 Y_1}{Y_2} + \frac{Y_5 Y_2}{Y_2} + \frac{Y_5 Y_3}{Y_2} + \frac{Y_5 Y_4}{Y_2} + \frac{Y_3 Y_2}{Y_2} \right]$$

$$V_i Y_1 = -V_o \left[\frac{Y_5 Y_1 + Y_5 Y_2 + Y_5 Y_3 + Y_5 Y_4 + Y_3 Y_2}{Y_2} \right]$$

$$\frac{V_o}{V_i} = \frac{Y_1 Y_2}{Y_5 Y_1 + Y_5 Y_2 + Y_5 Y_3 + Y_5 Y_4 + Y_3 Y_2} \quad \text{-----3}$$

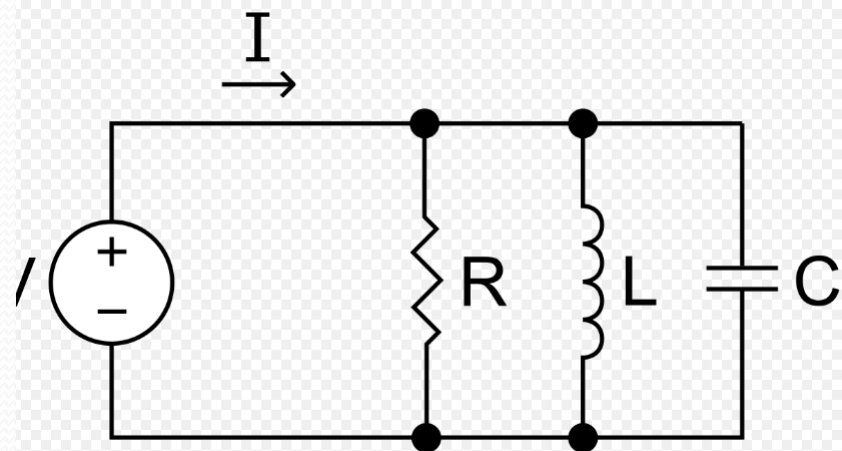
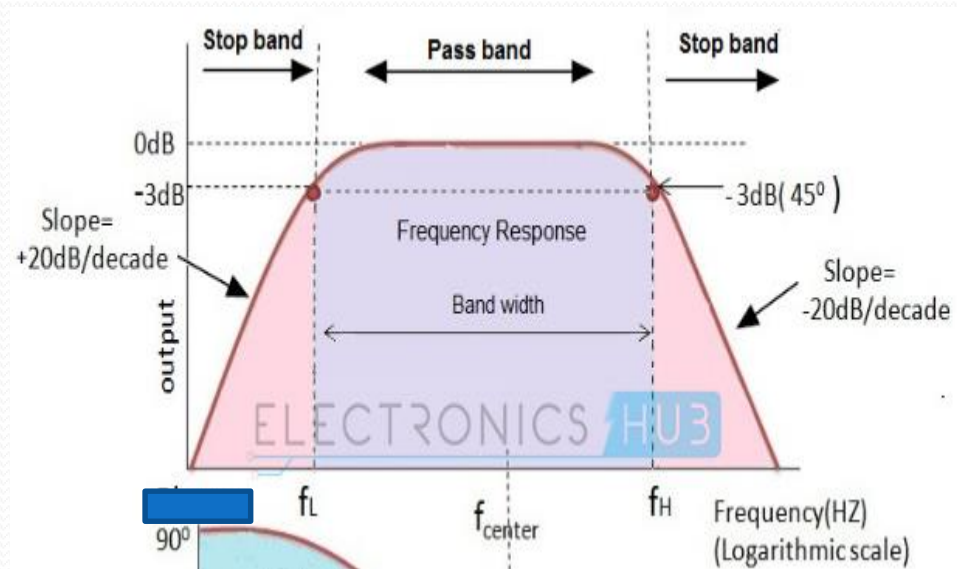
Acc to eqn A

$$\frac{V_o}{V_i} = \frac{-sG_1 C_2}{s^2 C_2 C_3 + G_1 G_5 + sC_2 G_5 + sC_3 G_5 + G_4 G_5}$$

$$\frac{V_o}{V_i} = \frac{-G_1}{sC_3 + \frac{[C_2 + C_3]G_5}{C_2} + \frac{G_5[G_1 + G_4]}{sC_2}} \quad \text{-----4}$$

TF is equivalent to parallel RLC circuit

$$\frac{V_o}{V_i} = \frac{-G'}{sC + \frac{1}{sL} + G} \quad \text{-----5}$$



Continued.....

- Compare 4 and 5,

$$G' = G_1$$

$$L = \frac{C_2}{G_5(G_1 + G_4)}$$

$$C = C_3$$

Resonance frequency for an RLC circuit, $\omega_0^2 = \frac{1}{LC}$

$$\omega_0^2 = \frac{G_5(G_1 + G_4)}{C_2 C_3} \text{-----6}$$

At resonance, $sL = 1/sC$

Then eqn 5 is V_o/V_i at $\omega = \omega_0$, $\frac{-G'}{G} = -\frac{G_1}{G_5(C_2 + C_3)/C_2} = \frac{-(\frac{G_1}{G_5})C_2}{C_2 + C_3}$

$$G_5 = 1/R_5; G_1 = 1/R_1 \quad = \frac{-(R_5/R_1)C_2}{C_2 + C_3}$$

Q factor at resonance $Q_0 = \frac{\omega_0 L}{R} = \omega_0 RC = \frac{\omega_0 C}{G} = \frac{\omega_0 C_2 C_3}{G_5(C_2 + C_3)} \text{-----7}$

$$BW = f_h - f_l = \frac{f_0}{Q_0} = \frac{\omega_0}{2\pi Q_0} = \frac{1}{2\pi RC} = \frac{G}{2\pi C}$$

$$BW = \frac{G_5(C_2 + C_3)}{2\pi C_2 C_3} \text{-----8}$$

$$f_0 = \sqrt{f_h f_l}$$

Continued.....

- At resonant frequency $C_2=C_3=C$

- $|V_o/V_i| = \frac{\left(-\frac{R_5}{R_1}\right)C}{C+C} = \frac{(-R_5)}{2R_1} = -A_0$ -----9

- $\omega_0^2 = \frac{G_5(G_1+G_4)}{C^2}$ -----10

- $BW = \frac{G_5(C_2+C_3)}{2\pi C_2 C_3} = \frac{G_5 * 2C}{2\pi C^2} = \frac{G_5}{\pi C} = \frac{1}{\pi R_5 C}$ -----11 damping factor, $\alpha = \frac{1}{Q}$

DESIGN OF THE FILTER:

Step 1: Choose $C_1=C_2=C$

Step 2: Resistors Calculation: $R_1 = \frac{Q}{2\pi f_c * C * A_f}$

$$R_2 = \frac{Q}{2\pi f_c * (2Q^2 - A_f)}$$

$$R_3 = \frac{Q}{\pi f_c * C}$$

Step 3: Gain at f_c : $A_f = \frac{R_3}{2R_1}$ Condn: $A_f < 2Q^2$

Step 4: For a multiple feedback filter, center frequency, f_c -new frequency f_c'

Without changing gain or BW. Replace R_2 by R_2'

$$R_2' = \left(\frac{f_c}{f_c'}\right)^2 R_2$$

Problems:

1. Design a narrow band pass filter $f_c=3\text{KHz}$, $Q=30$, $A_f=20$

Ans: Assume $C_1=C_2=C=0.1\mu\text{F}$

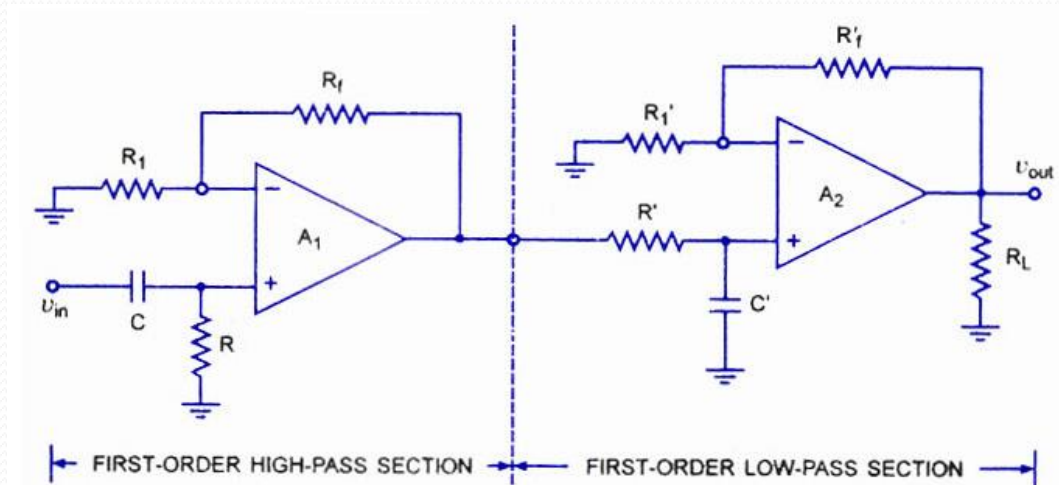
$$R_1 = \frac{Q}{2\pi f_c * C * A_f} = \frac{30}{2\pi * 3 * 10^3 * 0.1 * 10^{-6} * 20} = 796'\Omega$$

$$R_2 = \frac{Q}{2\pi f_c * (2Q^2 - A_f)} = \frac{30}{2\pi * 3 * 10^3 * (2 * 30^2 - 20)} = 9'\Omega$$

$$R_3 = \frac{Q}{\pi f_c * C} = \frac{Q}{\pi * 3 * 10^3 * 0.1 * 10^{-6}} = 32'\Omega$$

$$A_f = \frac{R_3}{2R_1}$$

WIDE BAND PASS FILTER:



Circuit Diagram

Wide Band Pass Filter

Continued....

- Cascading HPF and LPF
- If HPF and LPF are of first order, BPF will have a roll off rate-20dB/dec

- $|V_o/V_i| = \frac{A_o(\frac{f}{f_l})}{\sqrt{\left[1 + \left(\frac{f}{f_l}\right)^2\right] \left[1 + \left(\frac{f}{f_h}\right)^2\right]}}$ where $f_l = \frac{1}{2\pi RC}$ and $f_h = \frac{1}{2\pi R'C'}$

2. Design a wide band pass filter having $f_l = 400\text{Hz}$, $f_h = 2\text{KHz}$ and pass band gain of 4. Find value of Q

Ans: $A_o = 1 + R_f/R_i = 2$ so $R_f = R_i = 10\text{K}\Omega$

For LPF, $f_h = 2\text{KHz} = \frac{1}{2\pi R'C'}$ Let $C' = 0.01\mu\text{F}$, $R' = 7.9\text{K}\Omega$ Gain=2

For HPF, $f_l = 400\text{Hz} = \frac{1}{2\pi RC}$ Let $C = 0.01\mu\text{F}$, $R = 39.8\text{K}\Omega$ Gain=2

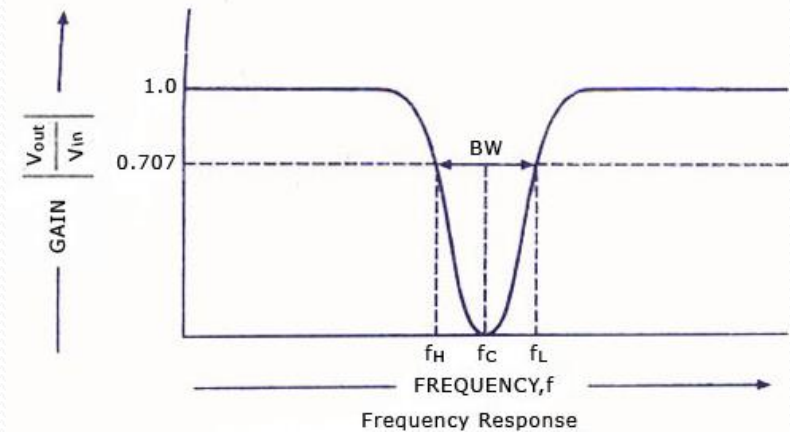
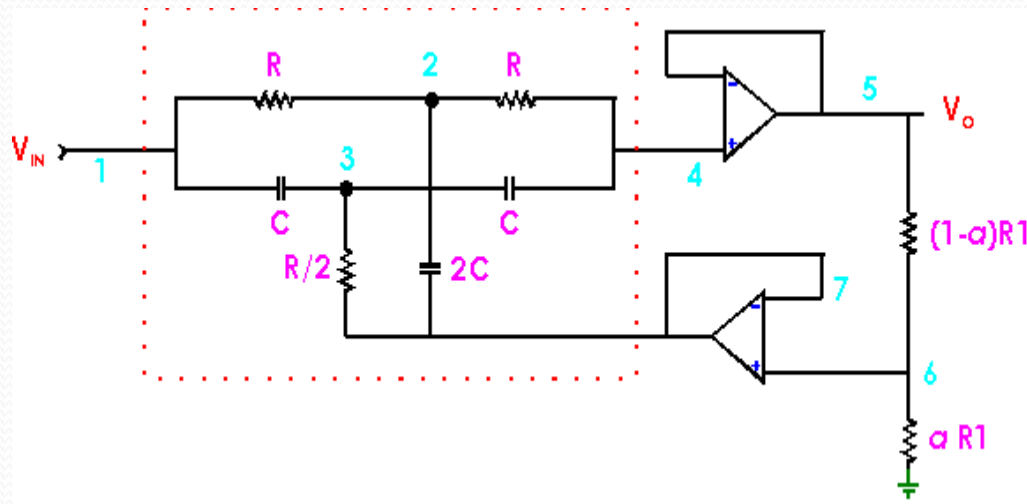
$$f_o = \sqrt{f_h f_l} = \sqrt{2000 * 400} = 894.4$$

$$Q = \frac{f_o}{BW} = \frac{f_o}{f_h - f_l} = \frac{894.4}{1800} = 0.56$$

For wide band pass filter, Q is very low, $Q < 10$

BAND REJECT FILTER

- Band stop /band elimination can be narrow/wide band
- Narrow band reject filter is called Notch filter(rejection of single frequency)
- Obtained by subtracting band pass filter o/p from its input



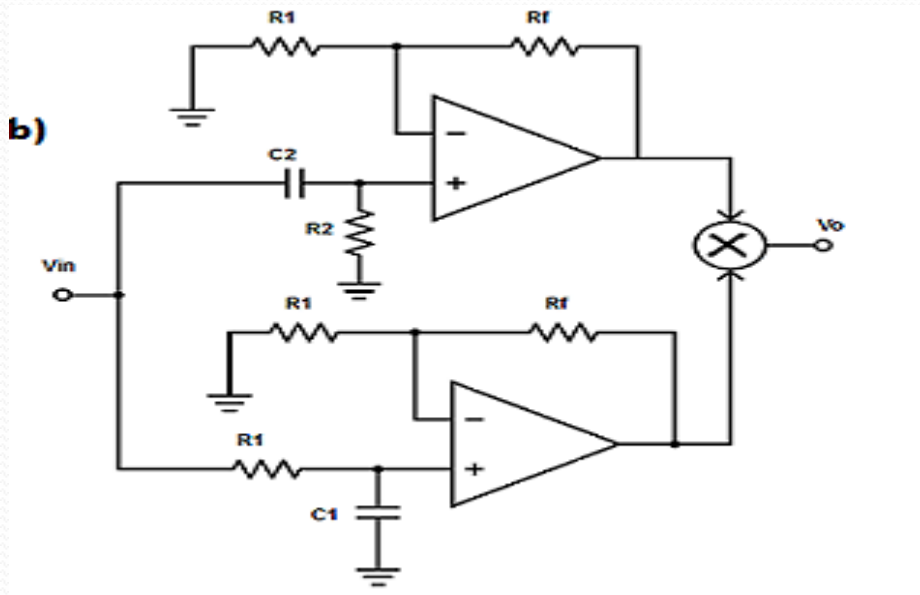
- $f_0 = \frac{1}{2\pi RC}$
- Design a 50Hz active notch filter

Ans: $f_0 = \frac{1}{2\pi RC} = 50\text{Hz}$ Let $C = 0.1\mu\text{F}$ $R = 31.8\text{K}\ \Omega$

For $R/2$ take two resistors of $31.8\text{K}\ \Omega$ in parallel and for $2C$ take two $0.1\mu\text{F}$ capacitors in parallel to make twin -T notch filter as shown above

Continued.....

- Wide band reject filter ($Q < 10$) made using a LPF, HPF and summer
- $f_l > f_h$ and pass band gain of LPF and HPF should be same



3. Design a wide band reject filter having $f_h = 400\text{Hz}$ and $f_l = 2\text{KHz}$ having pass band gain of 2

For HPF, $f_l = 2\text{KHz} = \frac{1}{2\pi R_2 C_2}$ Let $C_2 = 0.1\mu\text{F}$, $R_2 = 795\Omega$

For LPF, $f_h = 400\text{Hz} = \frac{1}{2\pi R_1 C_1}$ Let $C_1 = 0.1\mu\text{F}$, $R_1 = 3978\Omega$

$A_o = 1 + R_f/R_i = 2$ $R_f = R_i = 10\text{K}\Omega$

Questions:

1. Design a second order Butterworth Low Pass Filter with $f_H = 2\text{KHz}$
2. Design a first order wide bandpass filter with $f_H = 2\text{KHz}$ and $f_L = 500\text{ Hz}$
3. Design a Notch filter to eliminate power supply hum (50 Hz).
4. Design a Schmitt Trigger with hysteresis width, $V_h = 2\text{V}$.
Assume $V_{\text{sat}} = \pm 14\text{V}$
5. Design a circuit to generate 1KHz triangular wave with 5V peak.
6. Design a first order low pass filter at a cut-off frequency of 2kHz with a pass band gain of 3
7. Derive the design equations for a second order Butterworth active low pass filter
8. What is a zero crossing detector?
9. Derive the equation for frequency of oscillation for a square-triangular waveform generator.
10. Derive the equation for the transfer function of a first order wide Band Pass filter.